

# 6. Kinematic GPS and Applications

Tectonic Geodesy  
GEOS 655

# Kinematic GPS



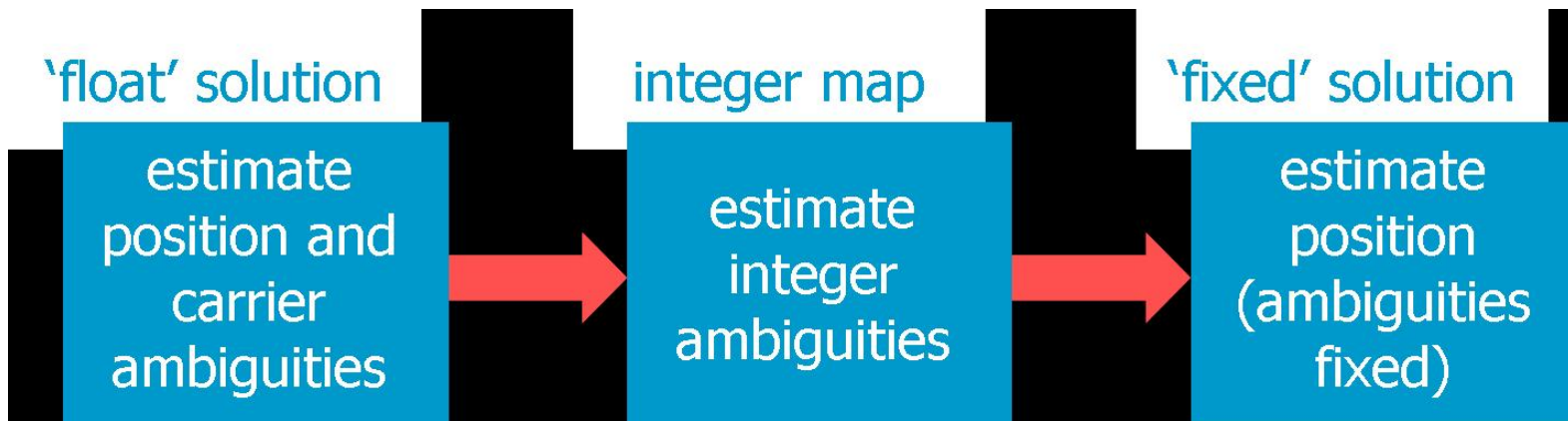
# Development of Kinematic GPS

- Research on GPS on kinematic platforms dates to 1980s.
- With ambiguities resolved, change in phase relates mainly to change in position.
- Demonstrated roughly centimeter-level positioning
  - Requires a fixed reference receiver near moving receiver.
  - Near means within a few to few tens of kilometers
- If you can position a vehicle, why not a site that moves because of dynamic earth/ice movements?
  - It took a while to recognize how precisely you can do it.
- But if you are interested in change in position over time, you may not need to resolve ambiguities.

# Present Applications

- Rapid surveying/vehicle tracking
  - At UAF: positioning the plane for glacier laser altimetry
- Seafloor geodesy (buoy tracking)
- Ice motion
  - sub-daily, diurnal, tidal fluctuations
- GPS Seismology
- Tidal studies (e.g., ocean loading)

# Ambiguity Resolution



- One way to estimate the ambiguities is to use a combination of phase and pseudorange, because the difference has only the ambiguity
- The difficulty with this is the noise level in the pseudorange data – you need to average for a while.
- The “float” solution has a real-valued estimate of ambiguity
  - The other complication is that there is an ambiguity for each frequency, but the ionosphere-free combination gives only one real-valued estimate (1 equation in 2 unknowns).

# Widelaning and Narrowlaning

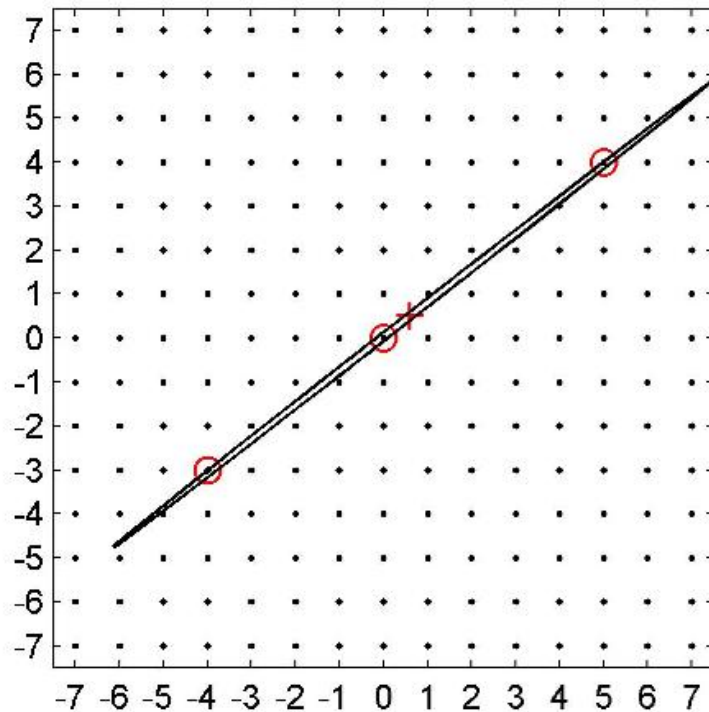
- There are some other linear combinations of the observables that are useful
  - Widelane:  $\phi_1 - \phi_2$  has wavelength  $\sim 86$  cm
  - Narrowlane:  $\phi_1 + \phi_2$  has wavelength  $\sim 10$  cm
  - The widelane ambiguity is particularly useful for ambiguity resolution, because it is relatively easy to average the pseudorange data down to give an estimate of the widelane ambiguity.
  - You can also estimate the widelane ambiguity by assuming that the (double-differenced) ionospheric delay is zero

# Static Solution Ambiguity Resolution

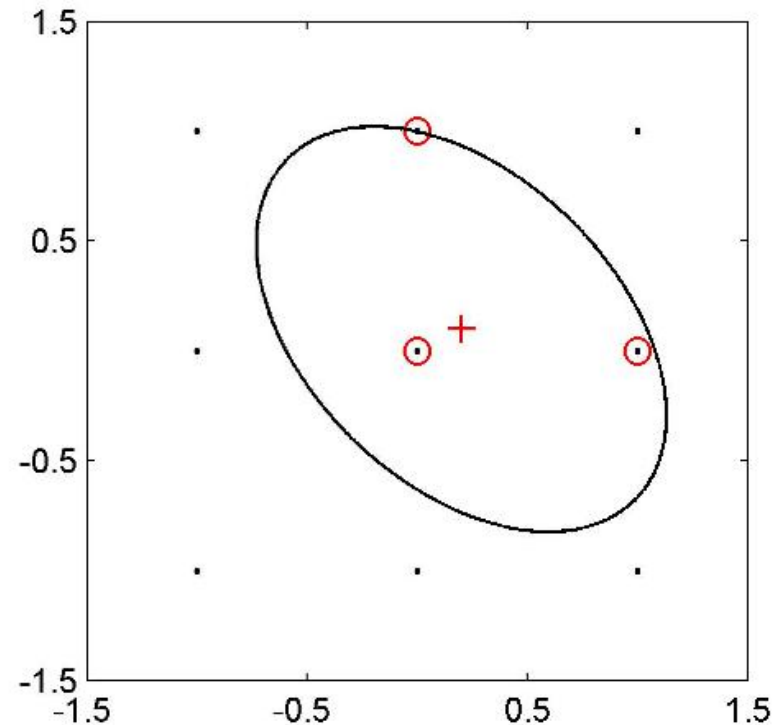
- Estimate float solution
- Resolve widelane ambiguities using
  - Pseudorange data
  - Ionosphere constraint
- Use fixed widelane bias and ionosphere-free bias estimate:
  - $B_{LC} = -n_1 f_1^2 / (f_2^2 - f_1^2) + n_2 f_2^2 / (f_2^2 - f_1^2)$
- Rewrite the above equation in terms of the widelane ambiguity:  $n_W = n_1 - n_2$

# Search-based Schemes

Identify possible candidate integer ambiguities based on “float” solution and covariance. Search all plausible candidates and find optimal.



True error ellipse



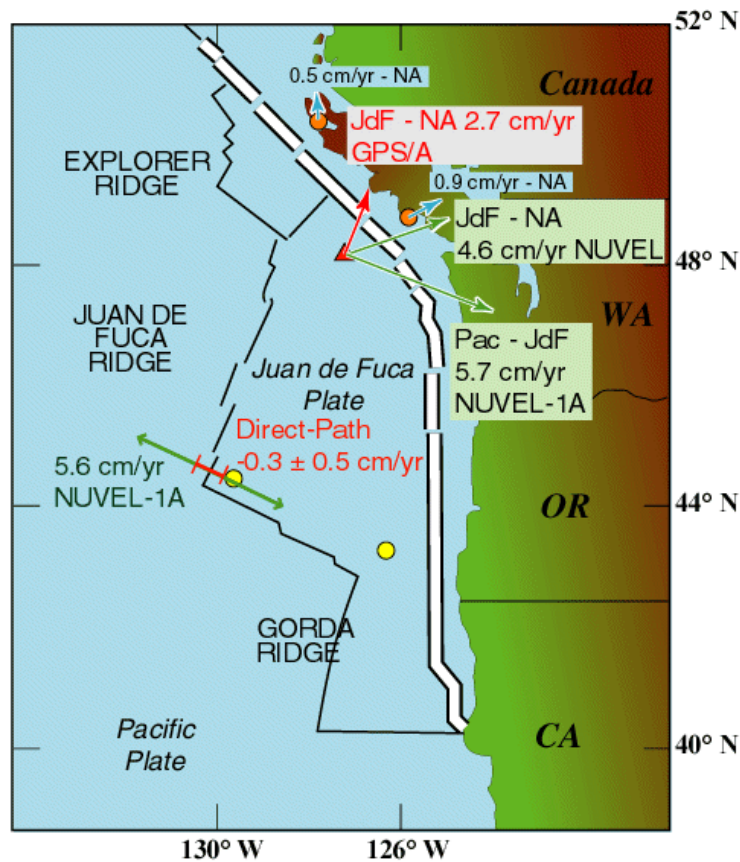
Decorrelated error ellipse



# Ambiguity Searches 2

- Ambiguity function
  - Maximize sum over all satellites and all epochs of data of function
    - $\text{Cos}(2*\pi*[\phi_{\text{obs}} - \phi_{\text{pred}}(x,y,z)])$
    - This term = 1 when predicted phase matches observed
  - Search is made by varying station position
- The key to any search-based method is to limit the number of candidates that must be searched.

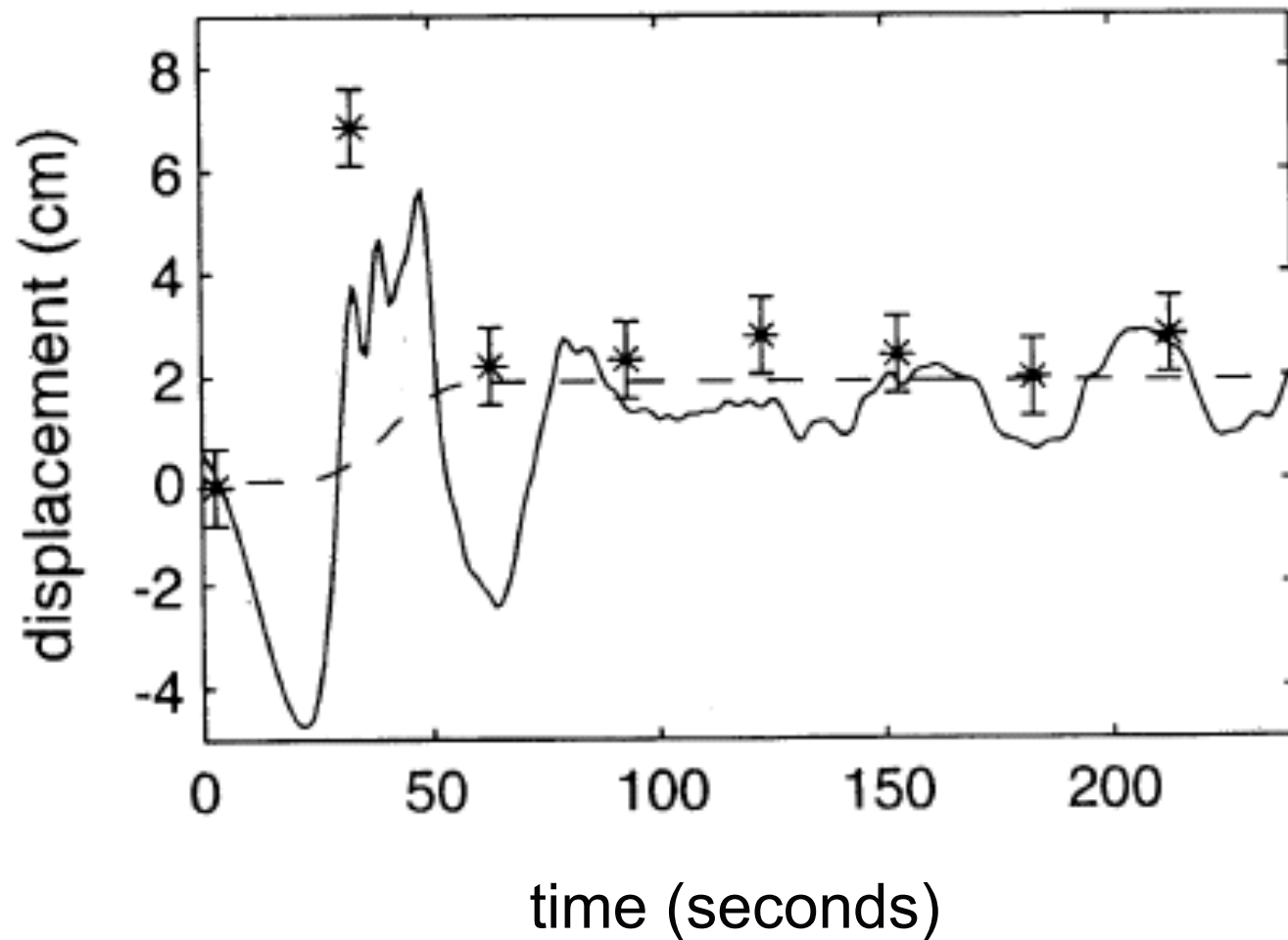
# Seafloor Geodesy



Chadwell et al., 1999

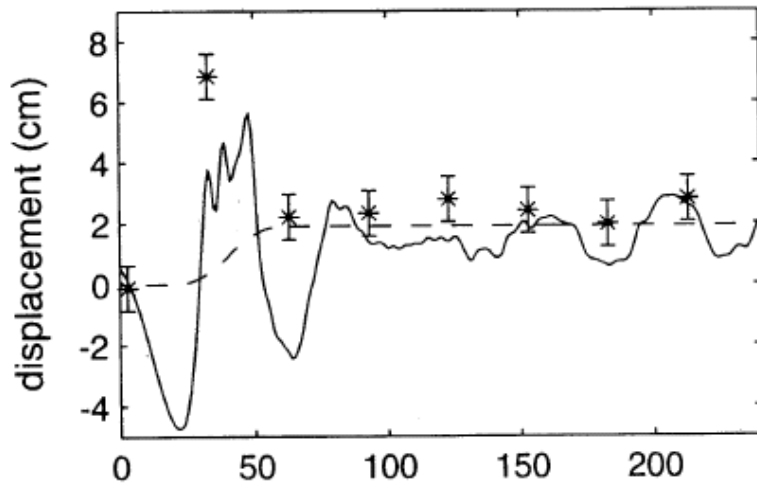
- Seafloor GPS project begun in early 1990s.
- GPS on buoy or ship
  - Positioned relative to satellites (GPS)
  - Positioned relative to seafloor transponders (acoustic)
  - Error mostly in water column velocity
- Measured Juan de Fuca convergence rate

# GPS Seismology - 30 s



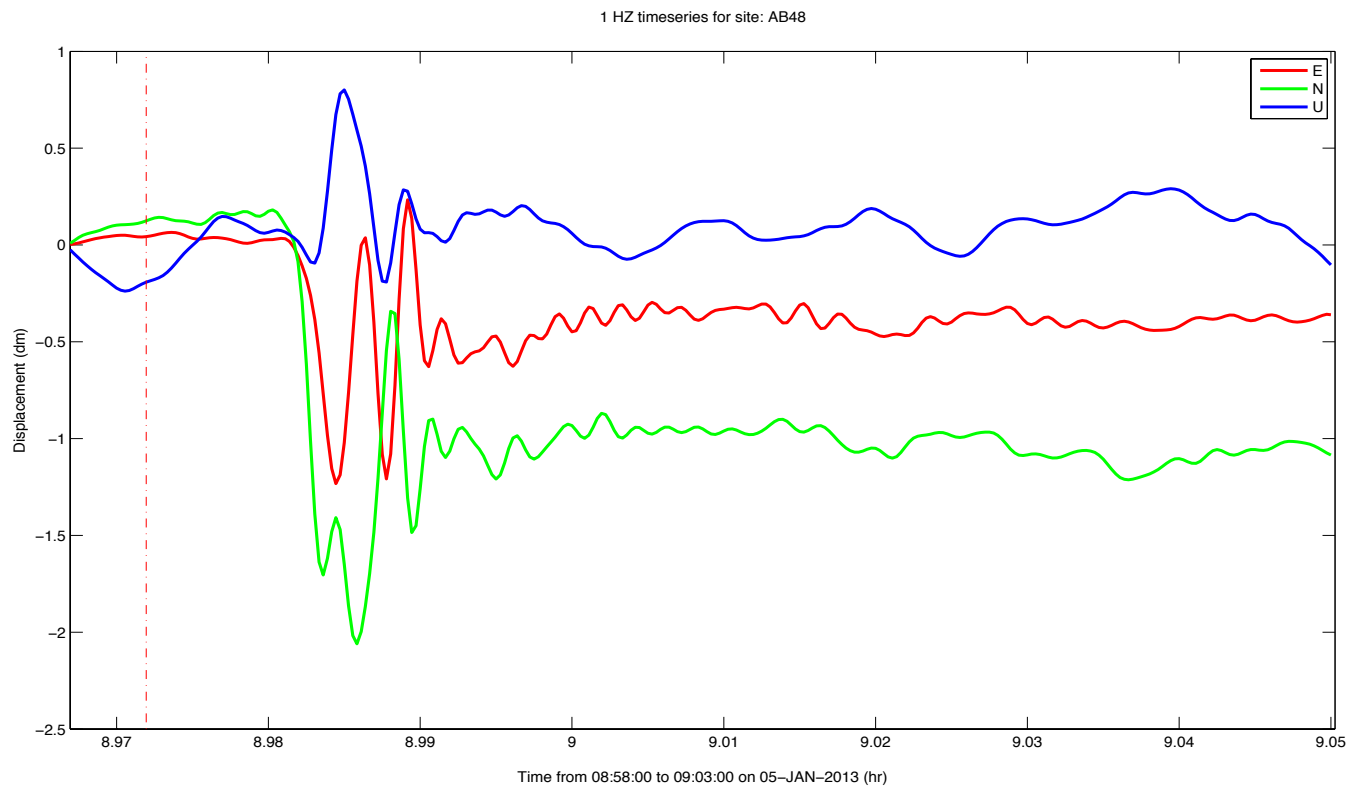
Hector Mine Earthquake     *Nikolaidis et al.*, 2001 (JGR).

# Nikolaïdis and Bock result



- Analyzed southern California data from time of 1999 Hector Mine earthquake
- Resolved ambiguities every epoch!
- Detected static displacement and transient point at time of seismic wave passage.

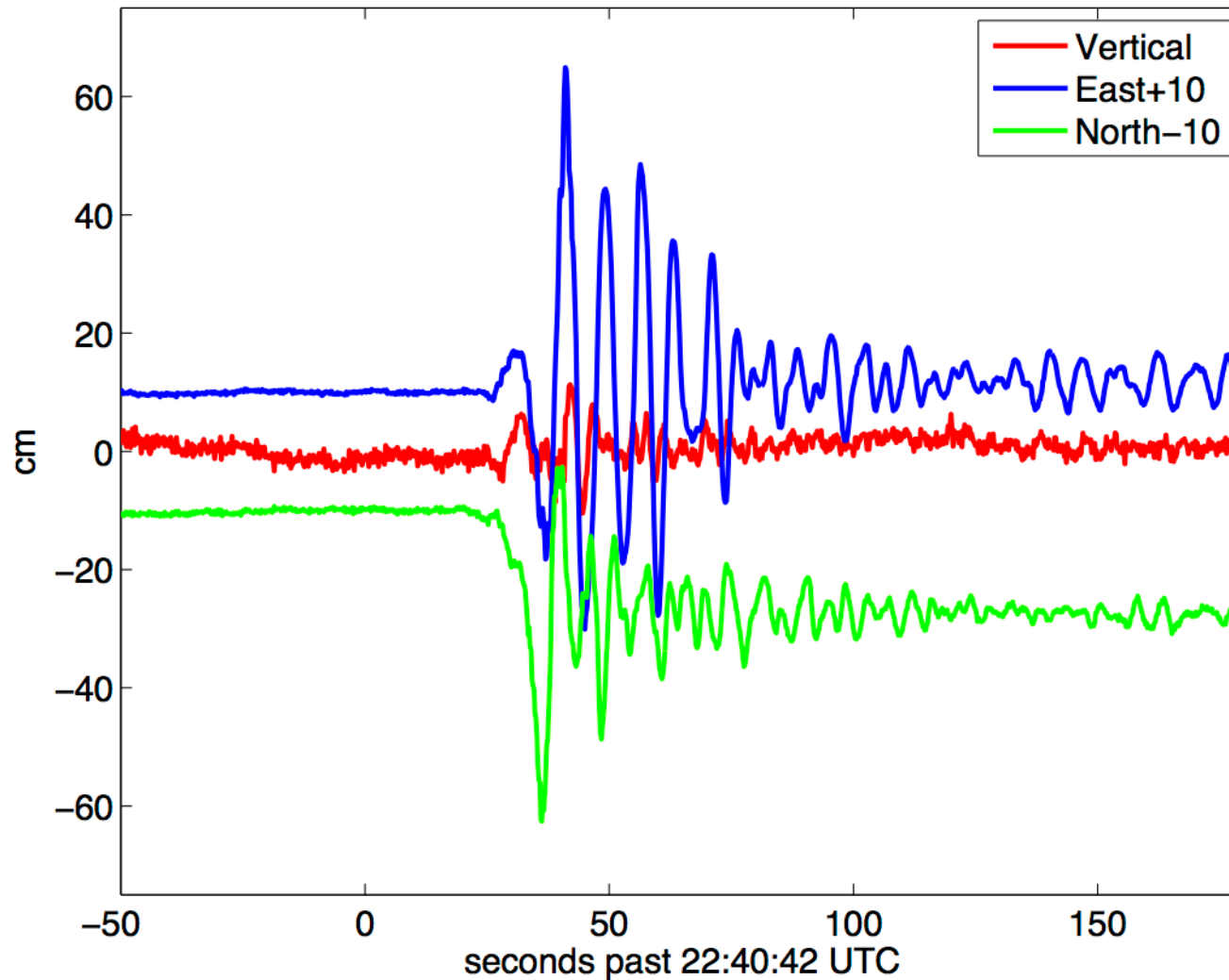
# 2013 Craig Earthquake



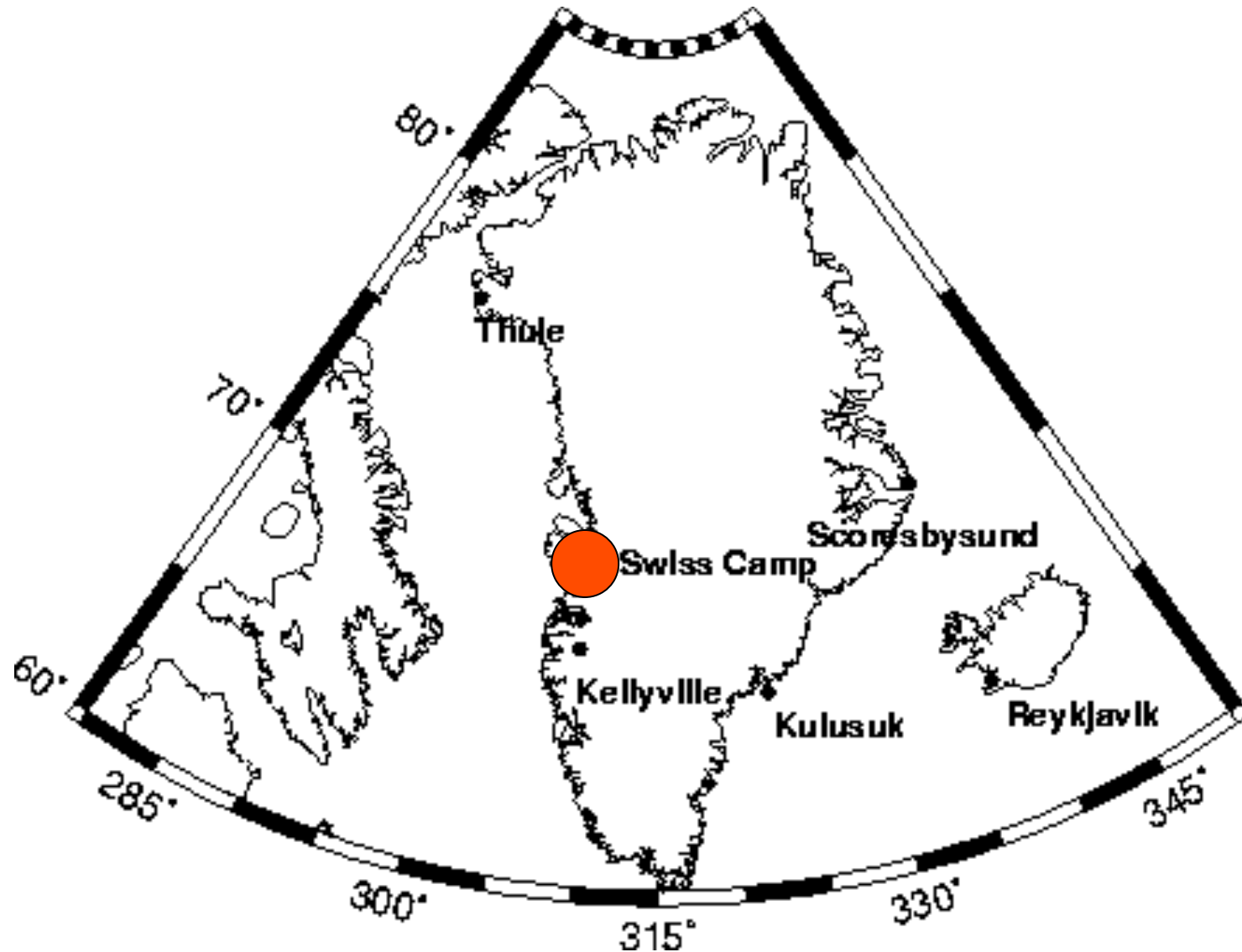
Kristine Larson  
*University of Colorado*

# El Mayor-Cucapah Earthquake

Baja Earthquake PBO Site p496y



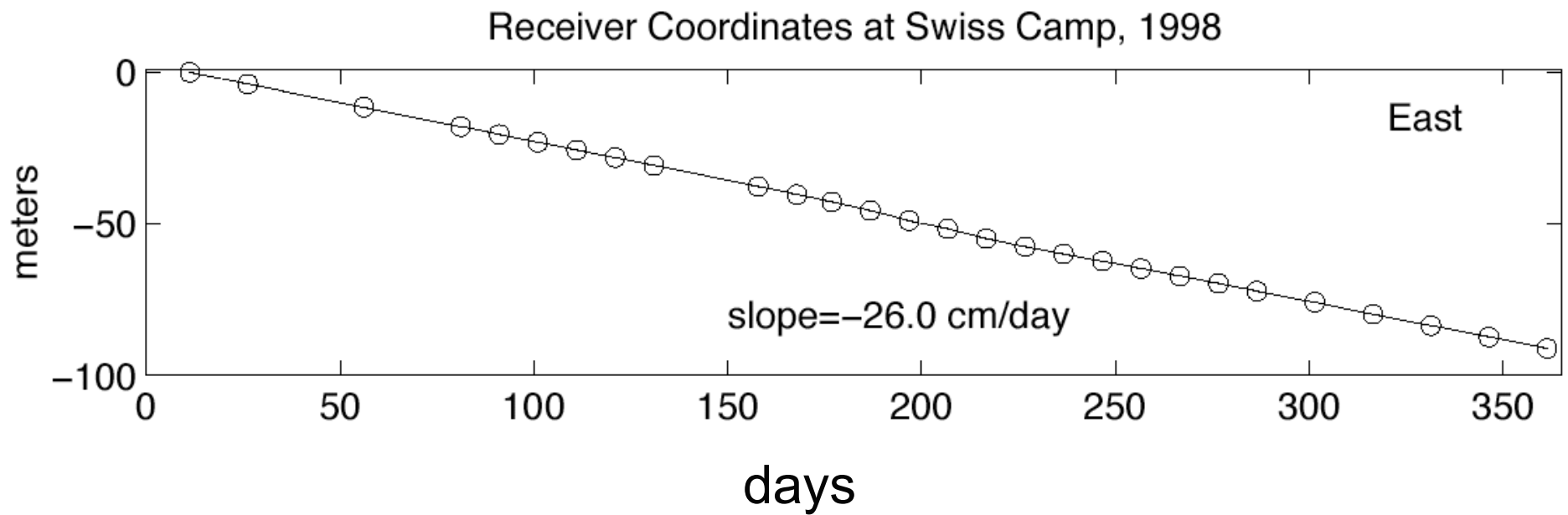
# Greenland Ice Sheet



Swiss Camp

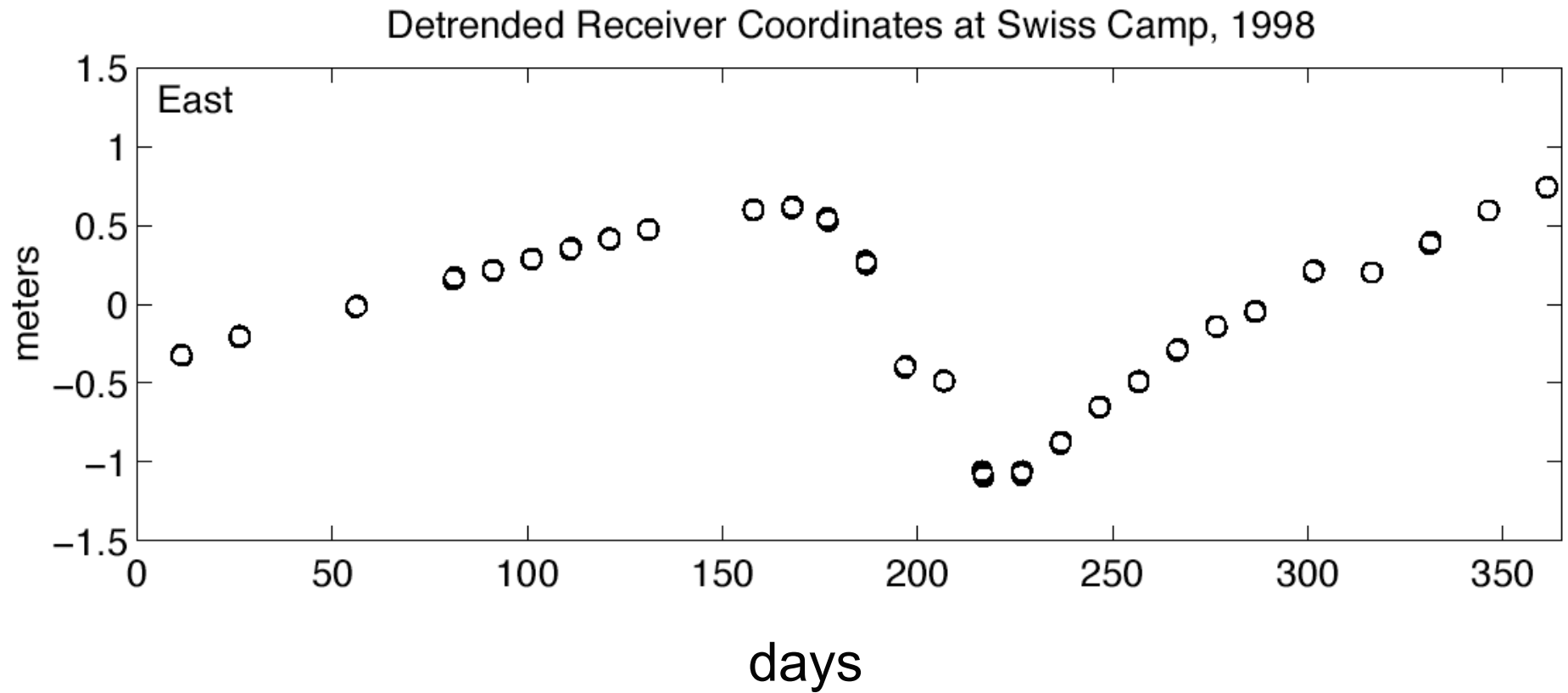
*Zwally et al., 2002, Science*

Full constellation; observations 10 hours every 10 days;  
Remove assumption that the receiver doesn't move.



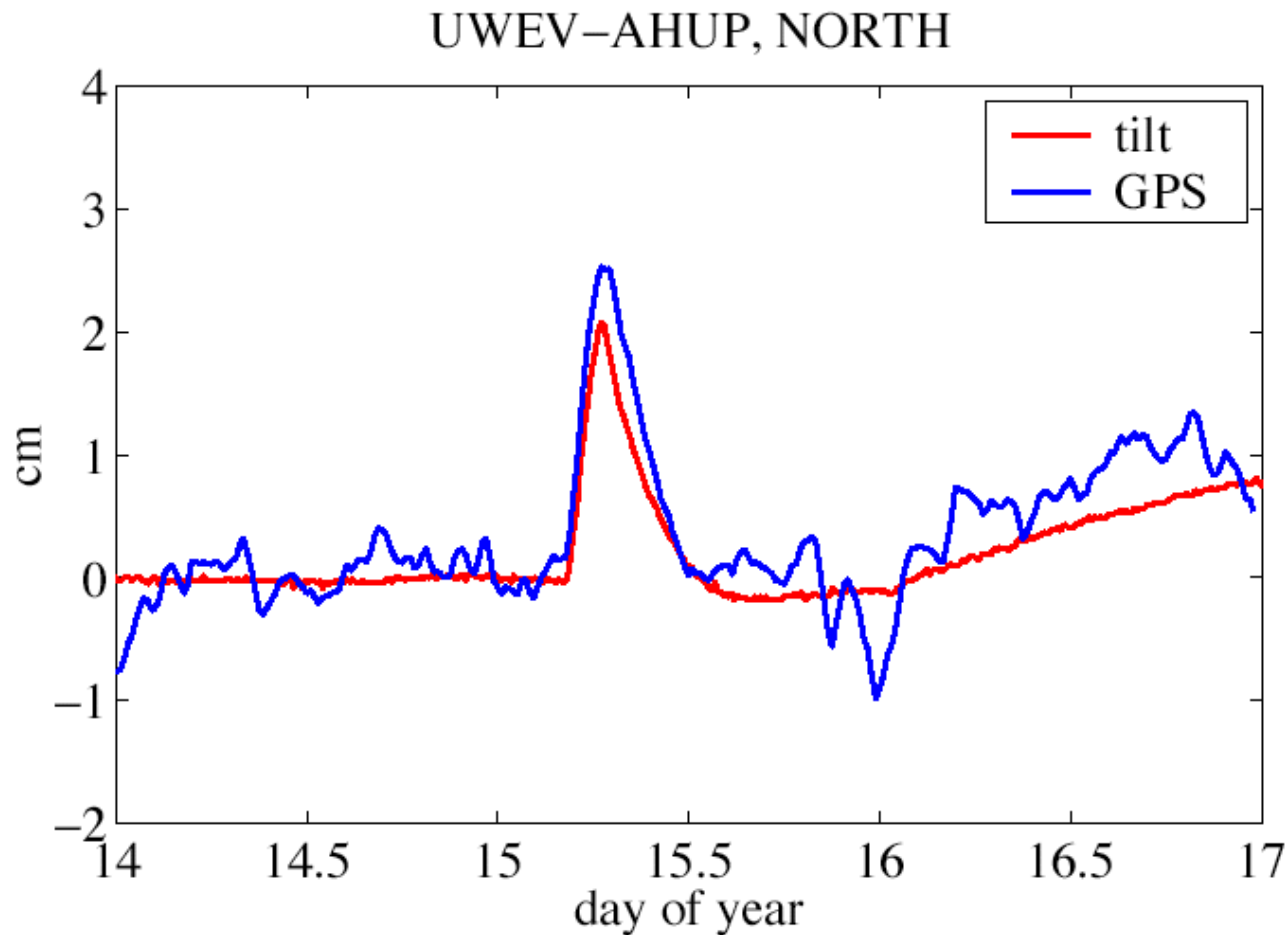


# Seasonal variations related to melt-water at the ice-rock interface.



# Volcano Monitoring

15 minute (filtered) averages of 5 minute observations

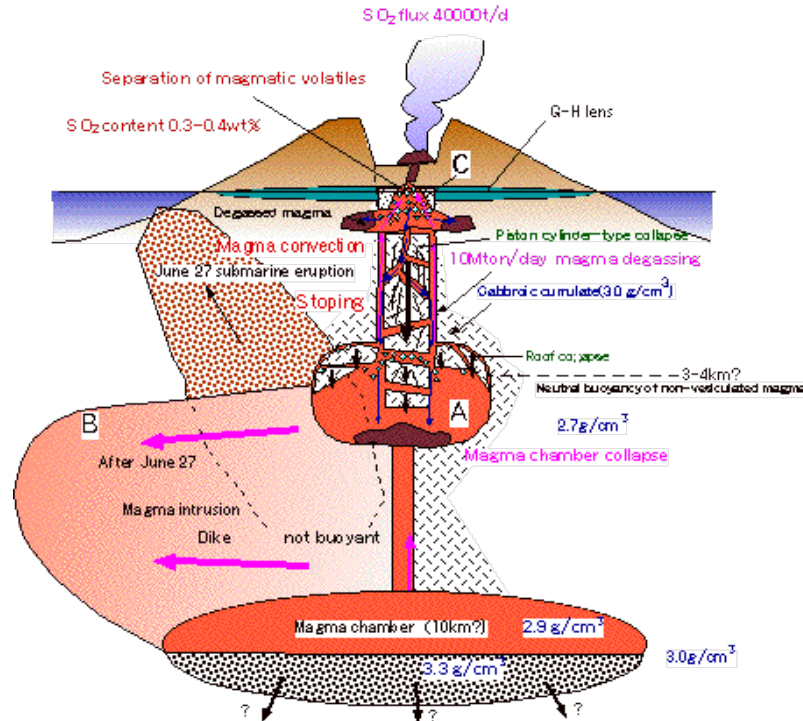


Kilauea Volcano

*Larson et al. (2001).*

# Miyakejima 2000 Eruption

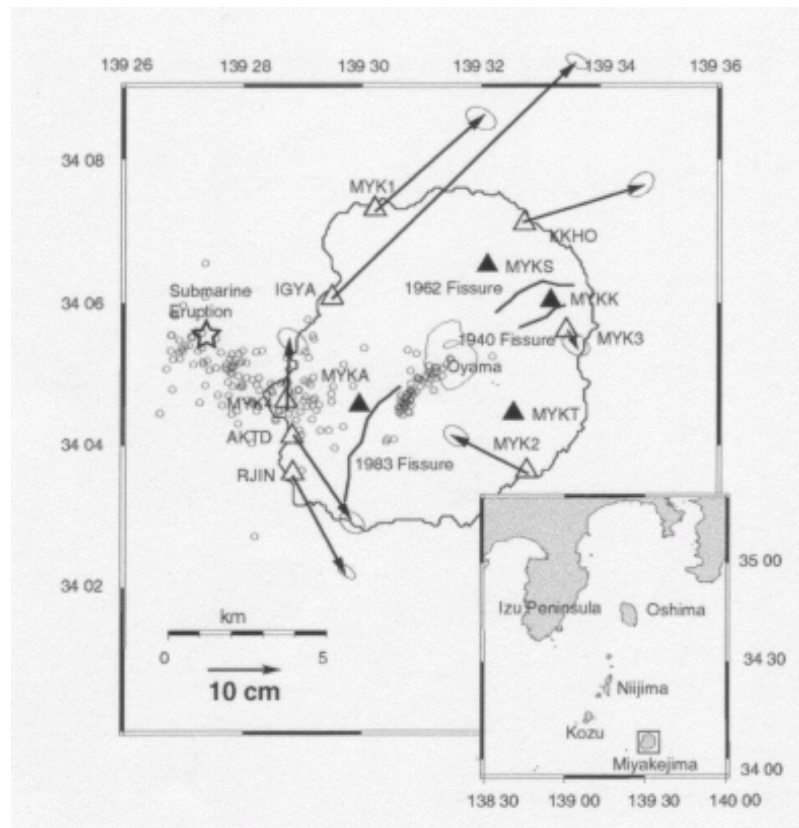
Schematic illustration of the Miyakejima volcanic processes



- Miyakejima in Izu Islands, off Japan
- Major volcanic event or year 2000 (June-August)
  - Seismic swarm
  - Small seafloor eruption
  - Large dike intrusion
  - Caldera collapse

Kazahaya et al., 2000

# GPS Displacements



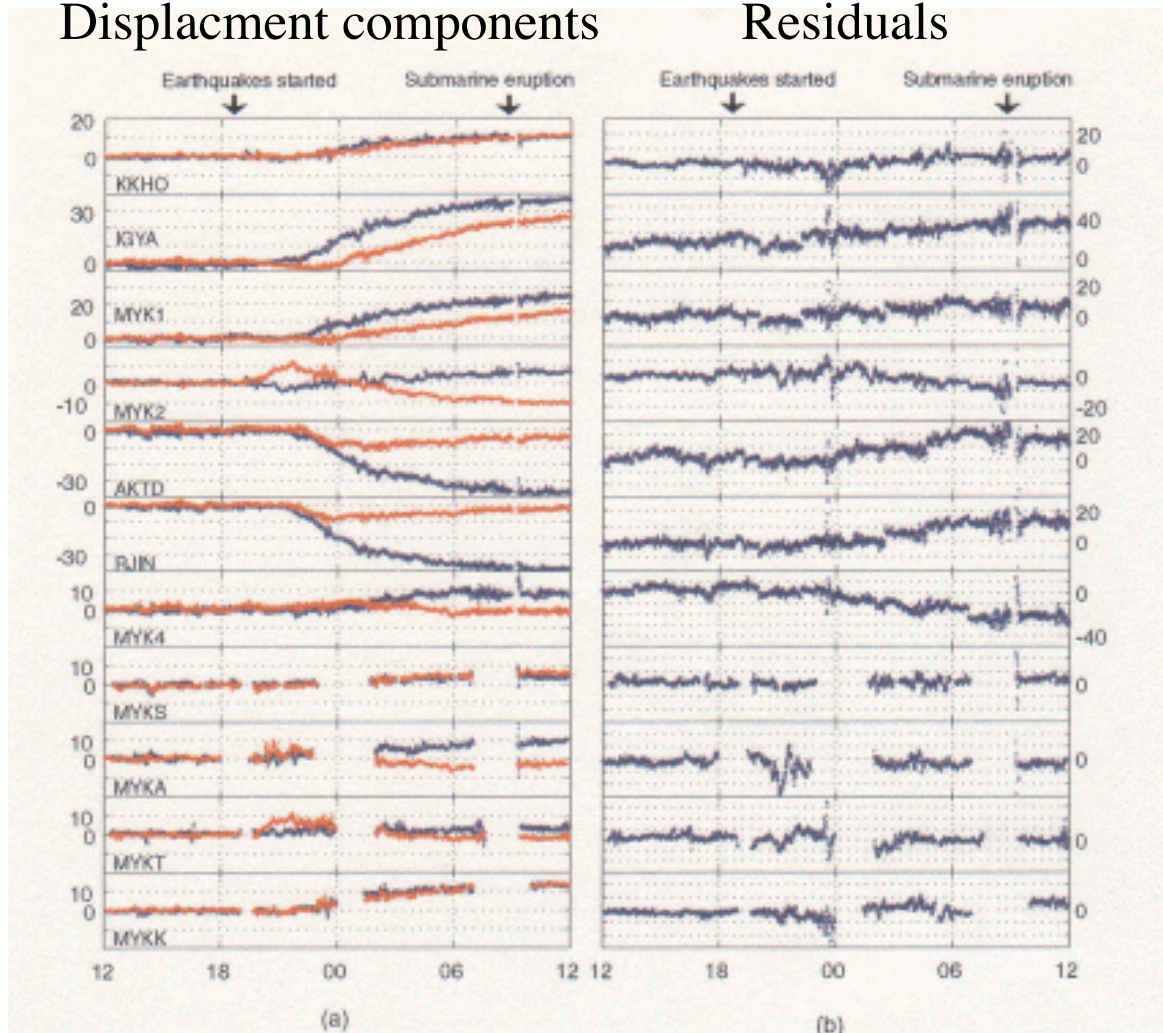
- Several continuous GPS sites on island, and on nearby islands
- Identified multiple phases in eruption from changes in deformation pattern
- Dramatic changes took place in first several hours.

Irwan et al., 2003

# Kinematic Displacement Records

Displacement components

Residuals



- Analyzed GPS data on an epoch-by-epoch basis.
- Provides a kinematic displacement record with ~30 sec resolution

## Why are GPS sites running at 1-Hz?

- NASA: low Earth orbit science missions.
- NGS: surveyors.
- Coast Guard (NGS): low precision navigation.
- FAA WAAS (wide area augmentation system): high precision real-time navigation.
- PBO Cascadia Initiative



# IGS Real-time Network



# GPS Static

- Sample at 30 sec.
- Edit data.
- Decimate to 5 min.
- Orbits are held fixed.
- Estimate one position per day.

# 1 Hz Kinematic

- Sample at 1 Hz
- Edit data.
- No decimation.
- Orbits are held fixed.
- Estimate one position per second.

The same software can be used to analyze the data in post-processing mode. There are also specialized kinematic solvers. Real time requires different software.



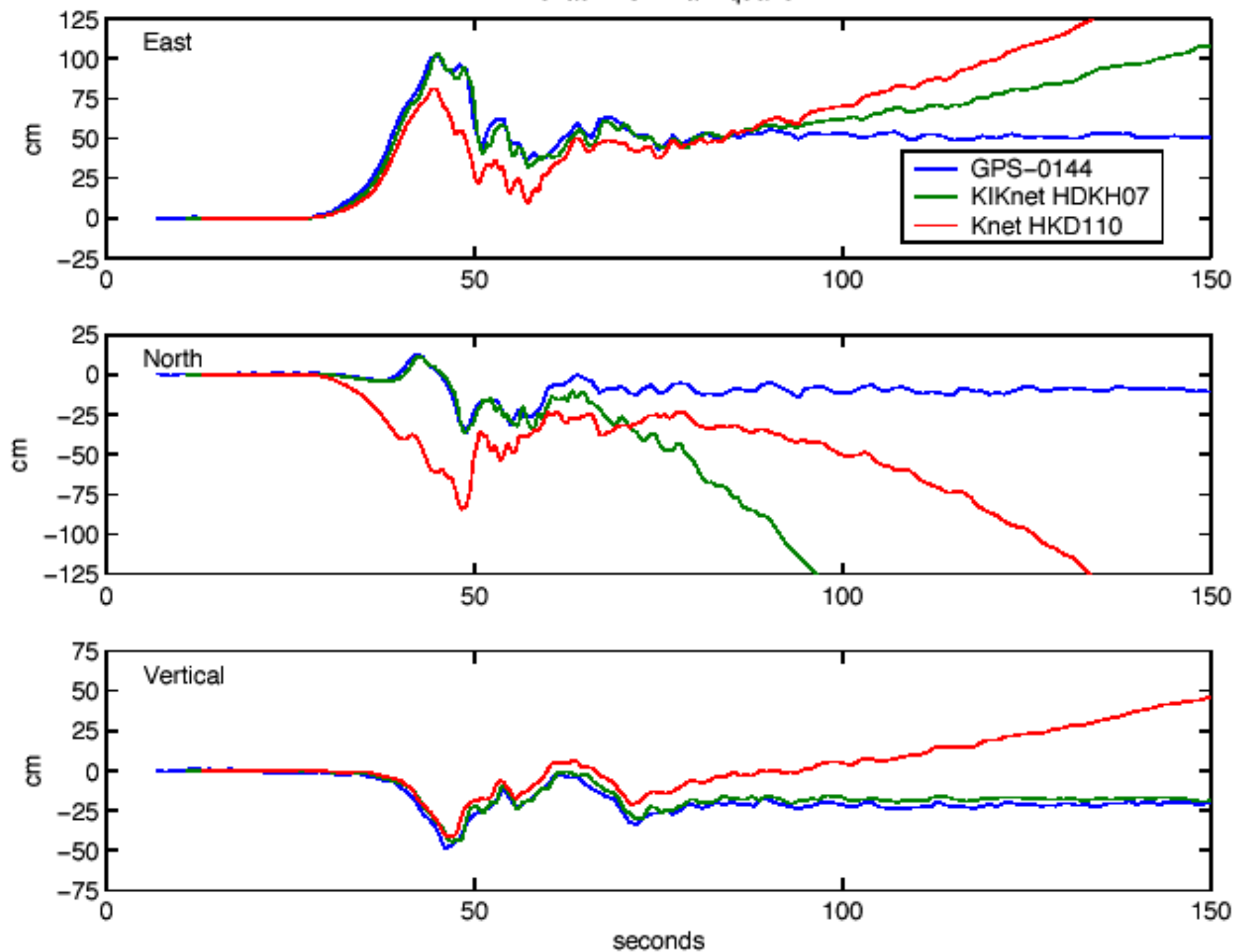
# 1 Hz GPS

- Relative ground motions [i.e. to a site held fixed]
- *Displacement* estimated
- Insensitive to small ground motions, but (almost) no upper limit...

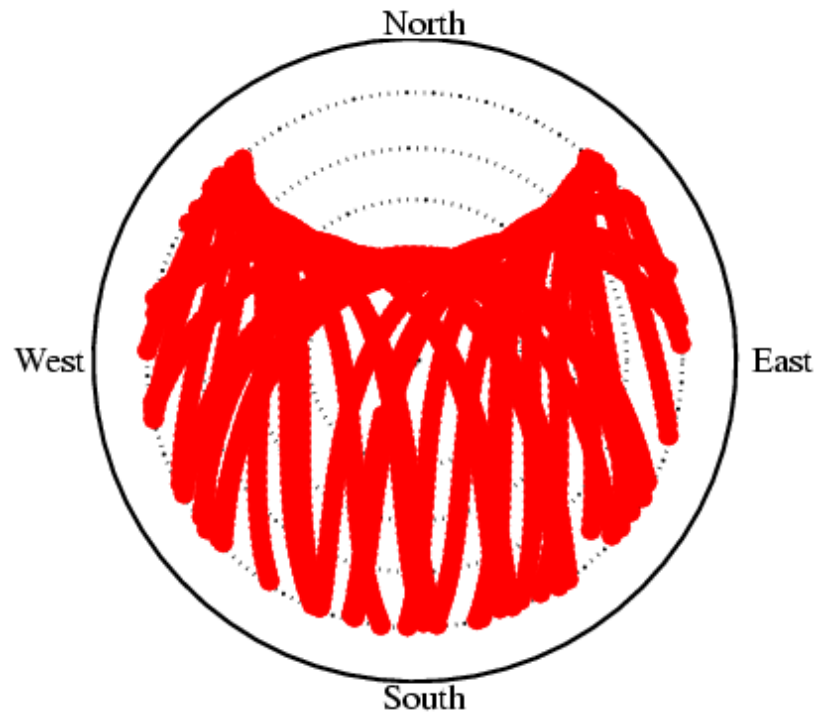
# Seismology

- Inertial local reference frame ground motions
- *Acceleration* measured
- Sensitive to small ground velocities or large accelerations

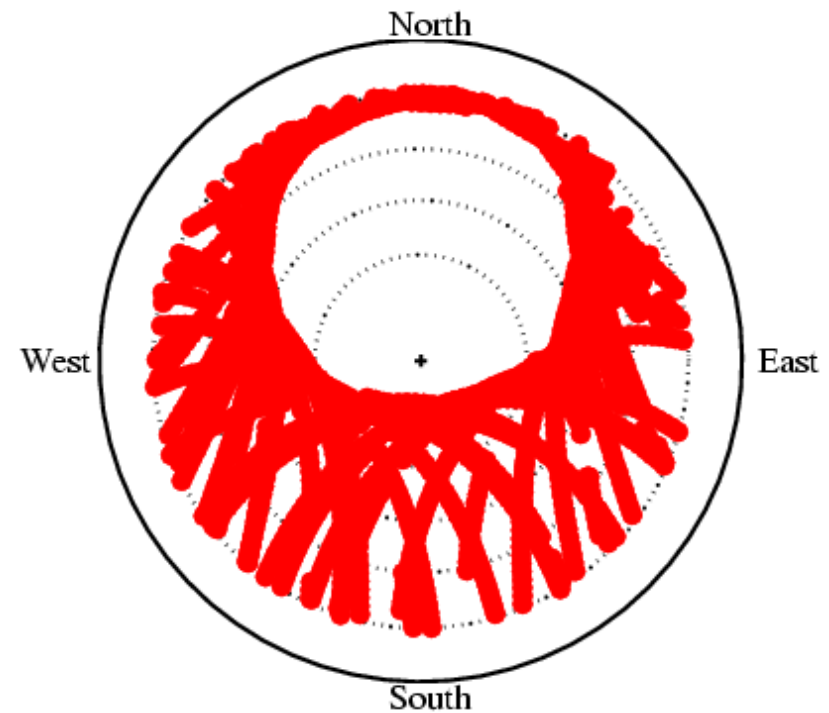
# Tokachi-Oki Earthquake



# 24 hours of GPS Data

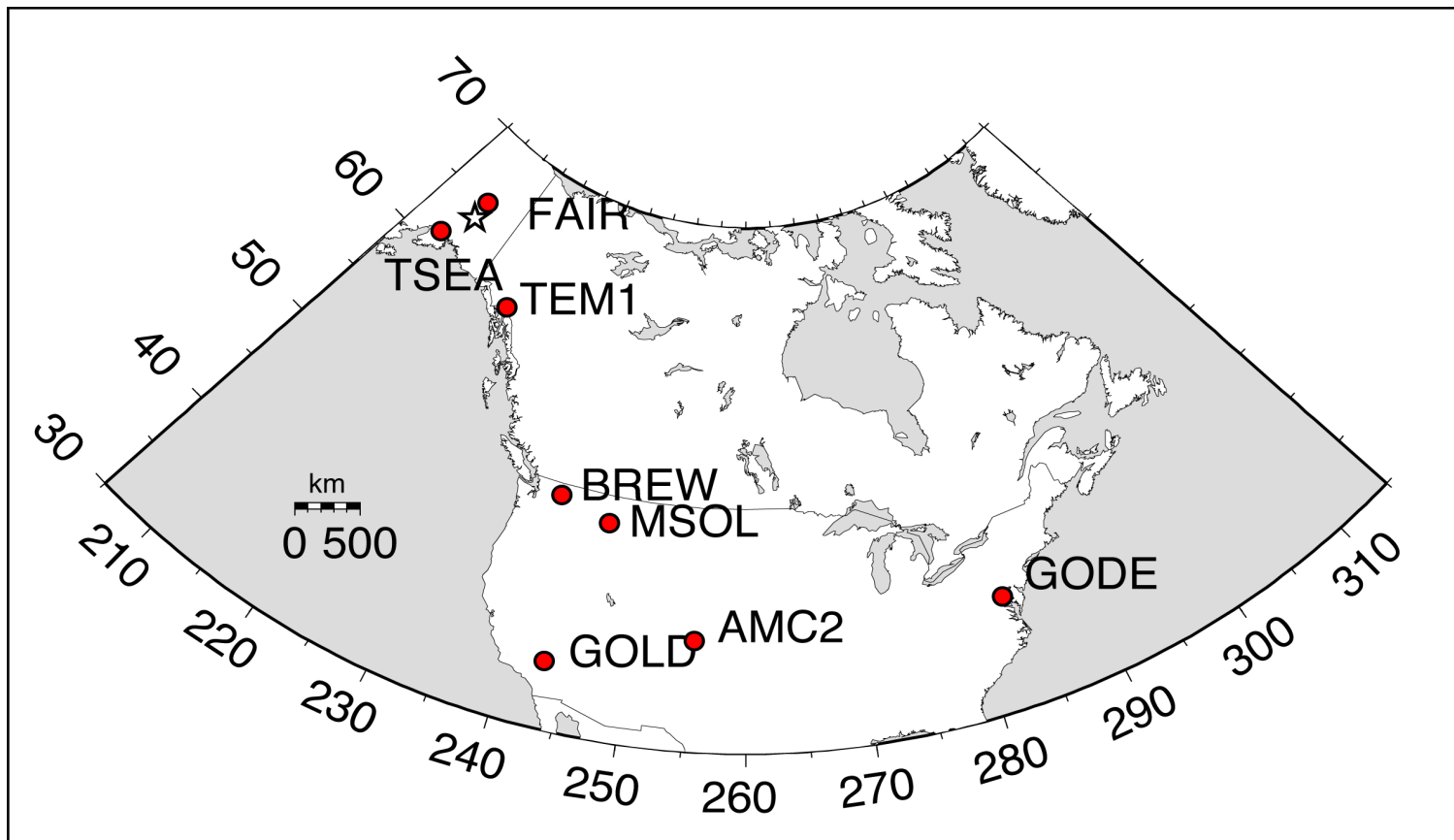


Southern California

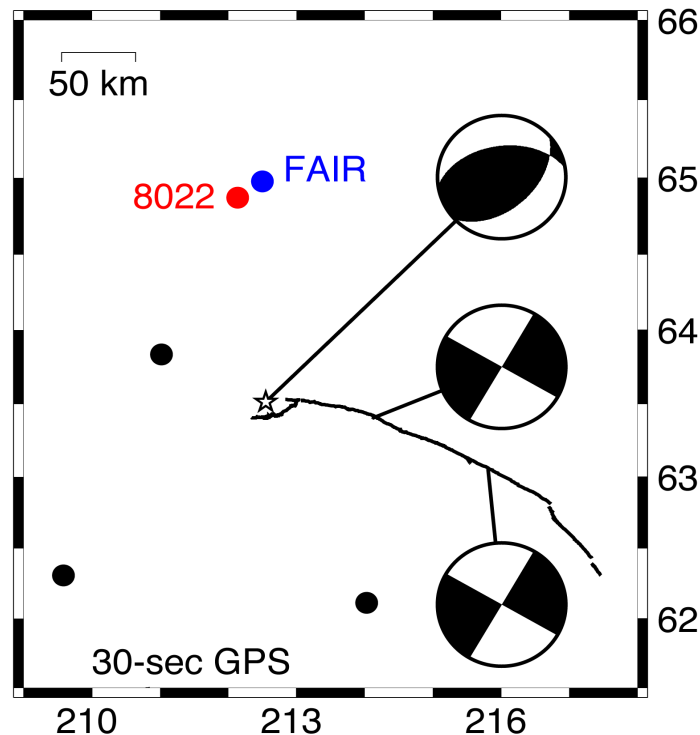


Fairbanks

# Original Denali GPS Network

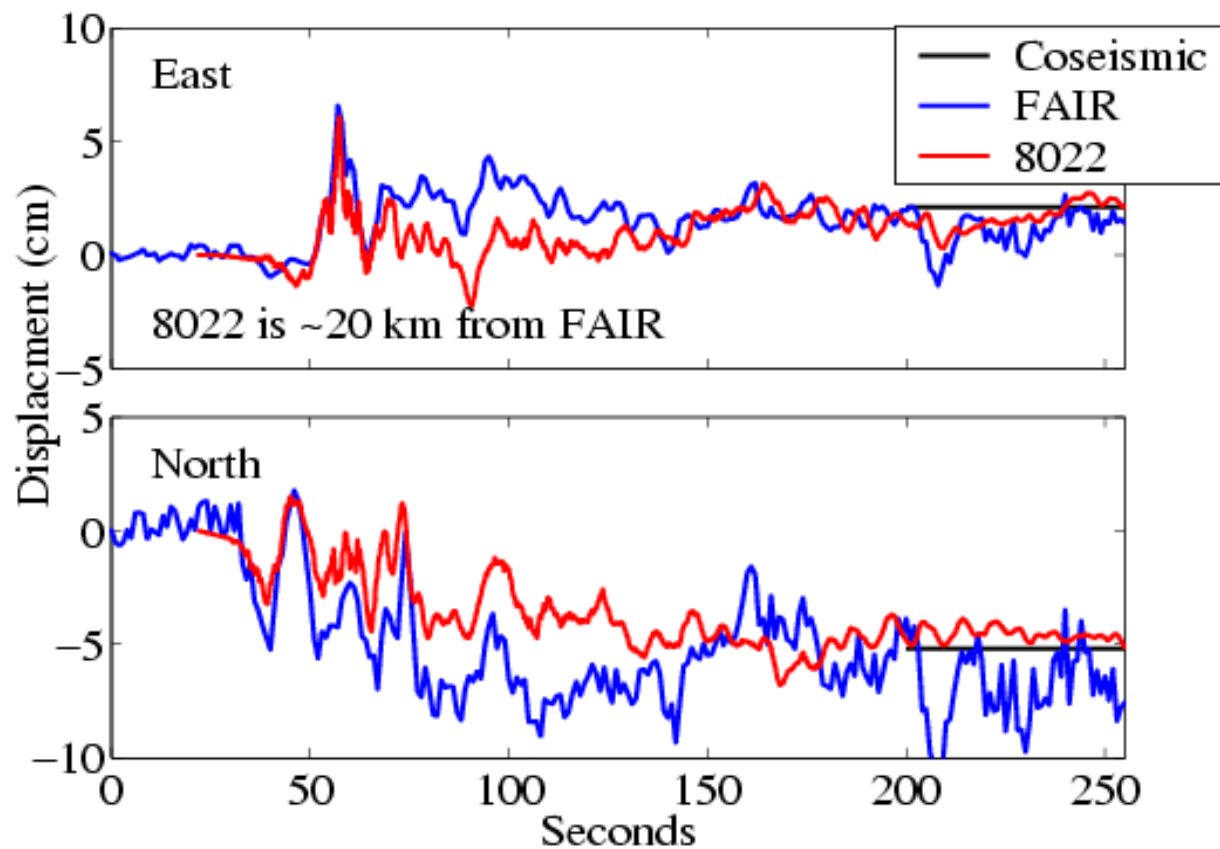


# Denali Fault earthquake

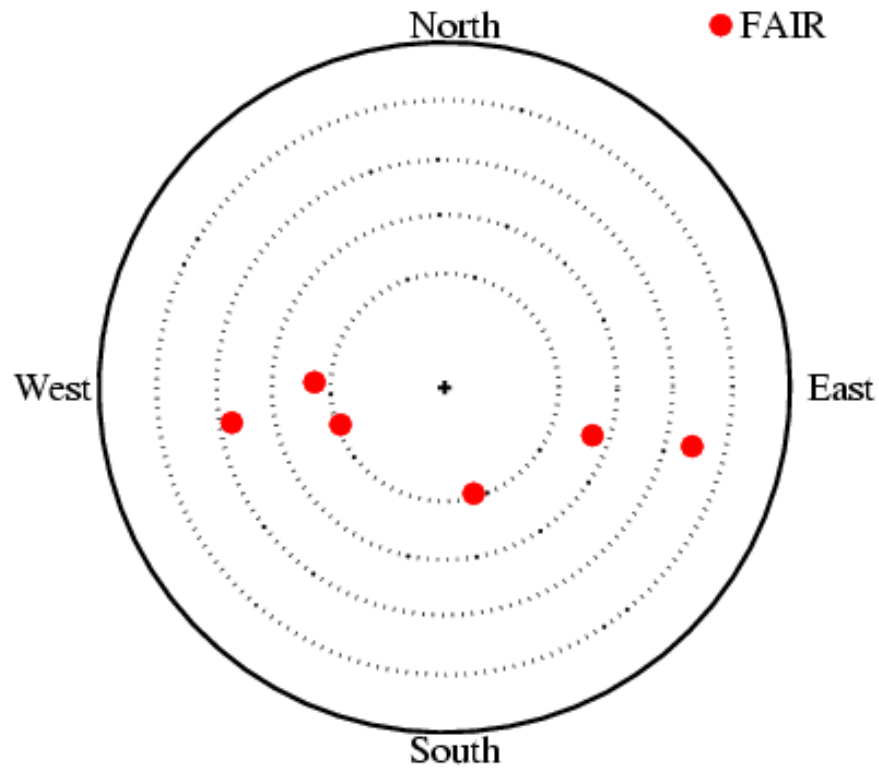


- 1 Hz GPS **FAIR**
- Strong motion **8022**
- High-pass filtered to remove baseline drift.
- Fix co-seismic offset [*Eberhart-Phillips et al.*, 2003]

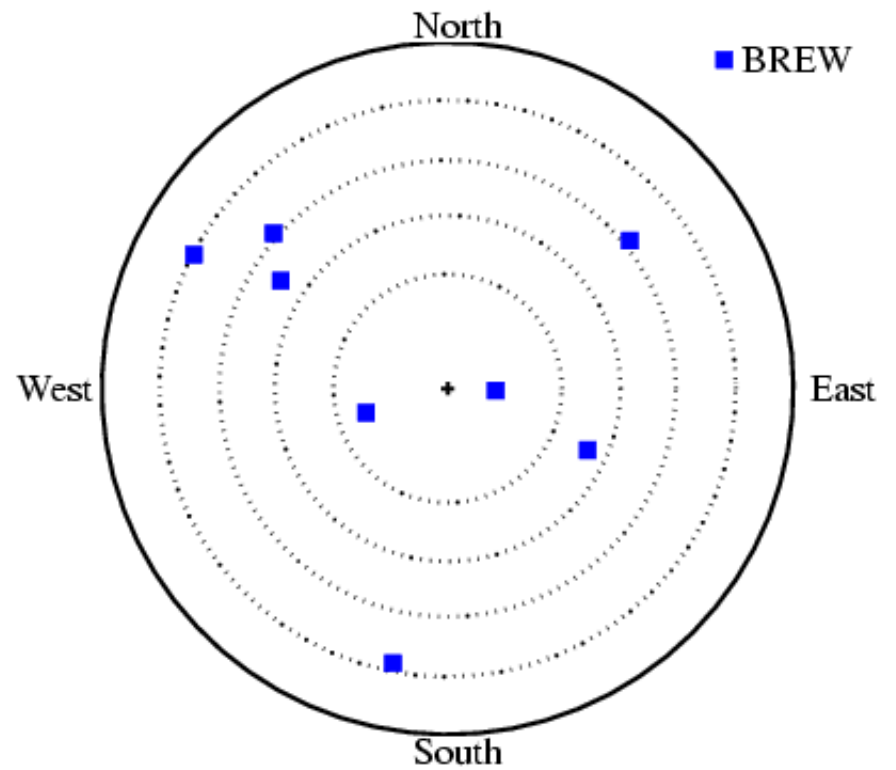
# 1 Hz GPS at FAIR



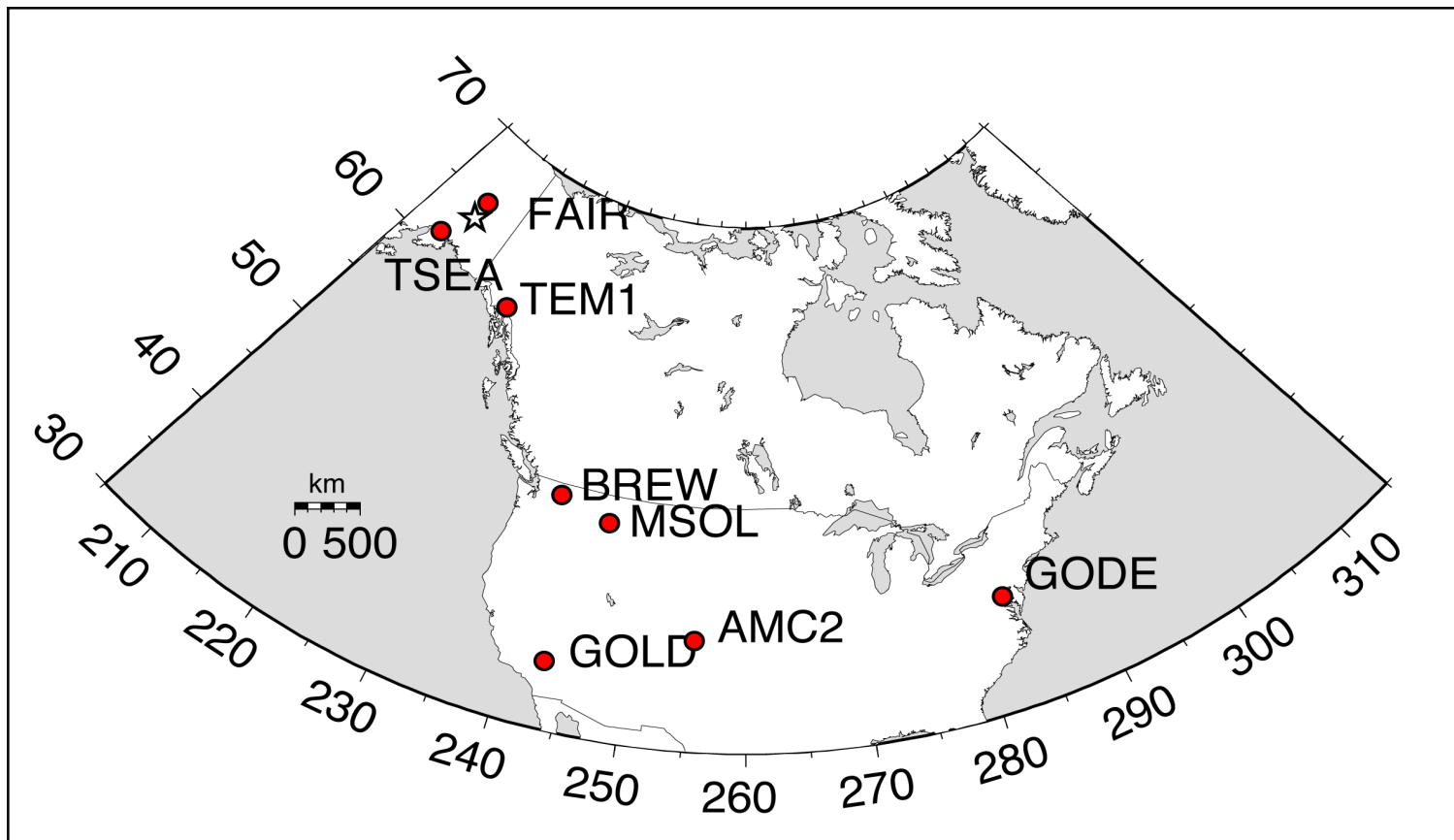
## FAIR



## BREW

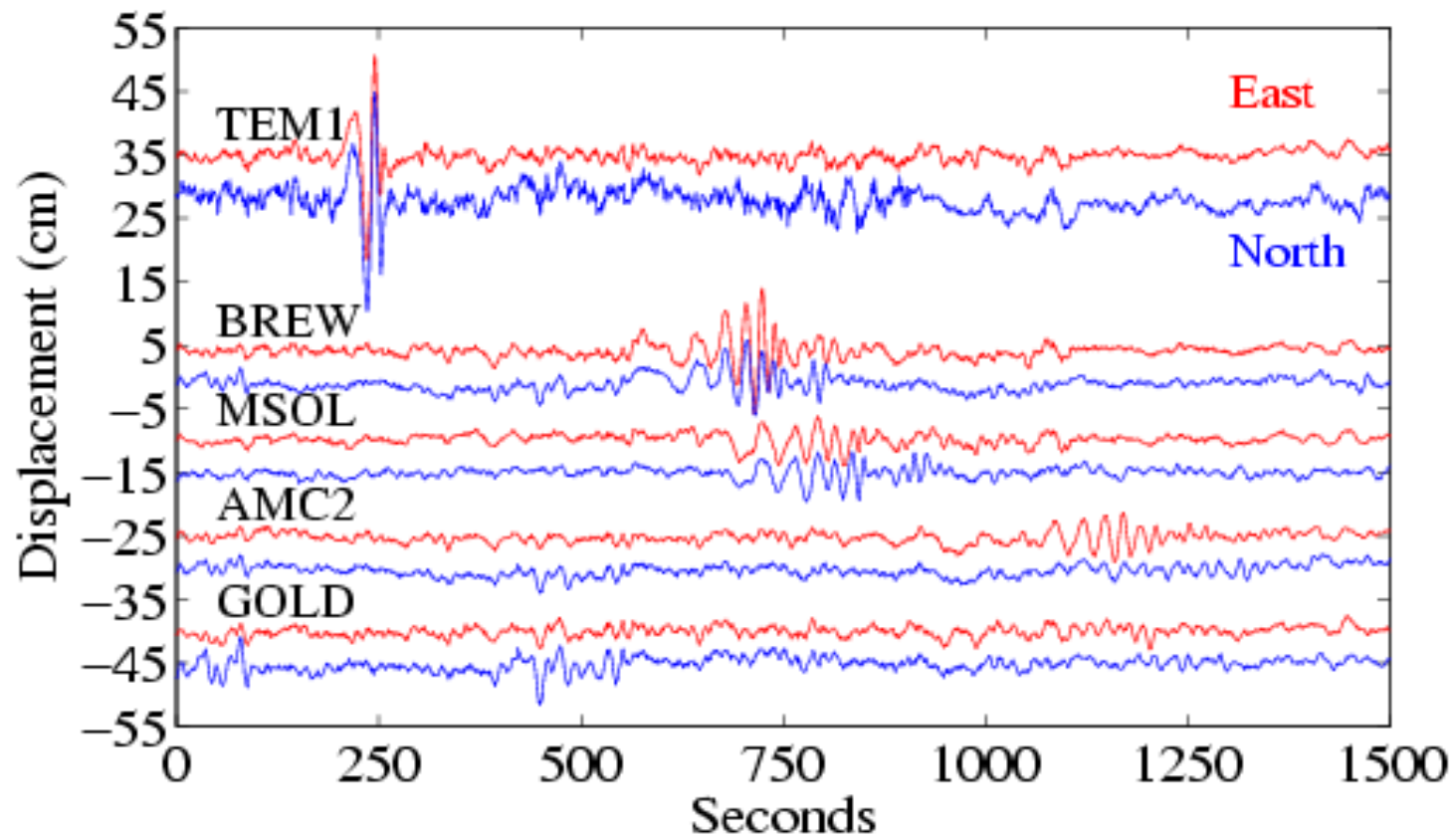


# Surface Wave Observations



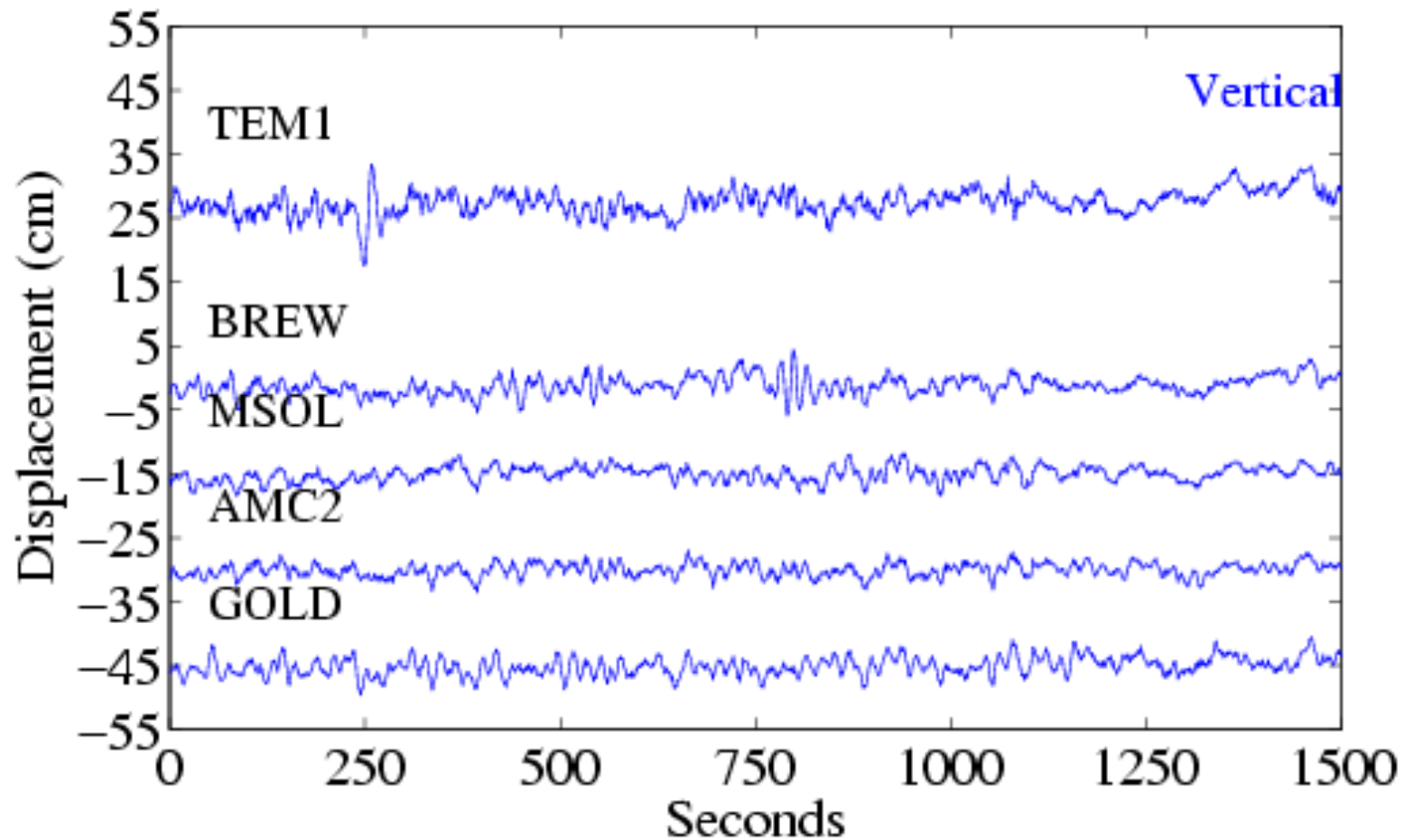


# GPS Surface Waves



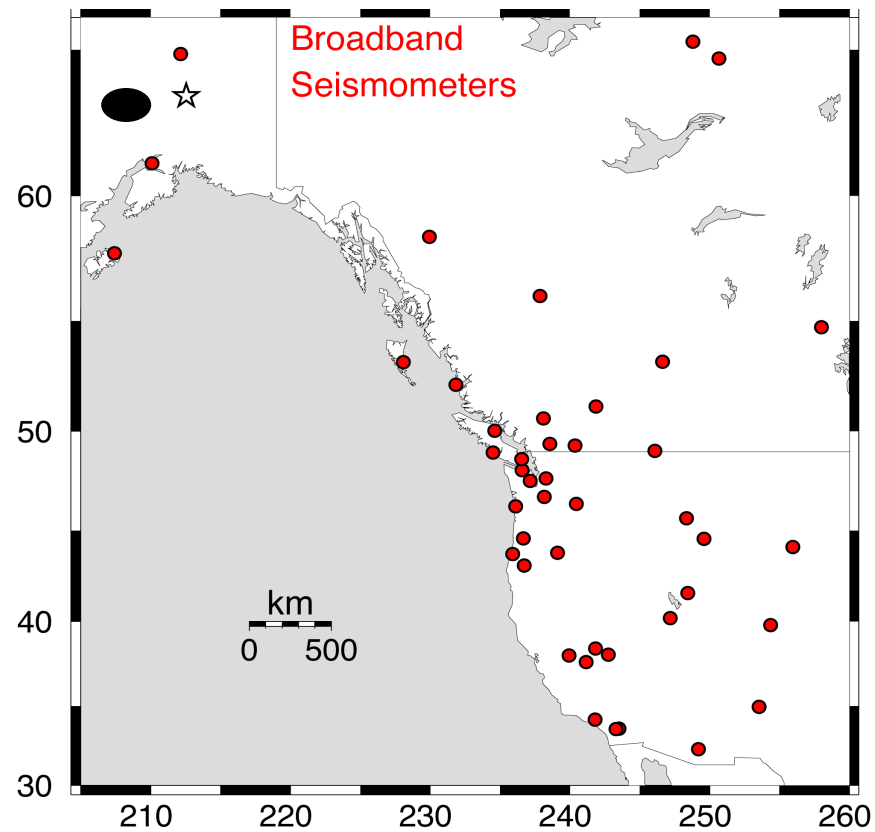
Larson et al., 2003, *Science*

# Can GPS do the vertical?

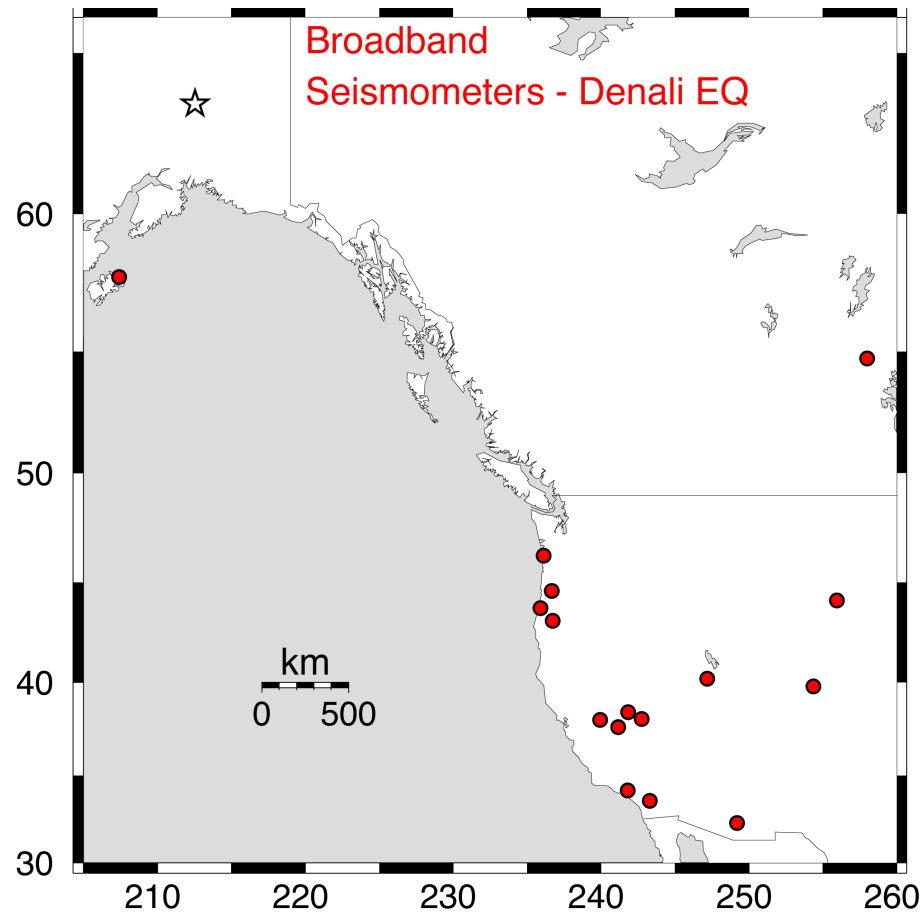


Yes, but not as well as the horizontals.

# Denali Seismic Instrumentation

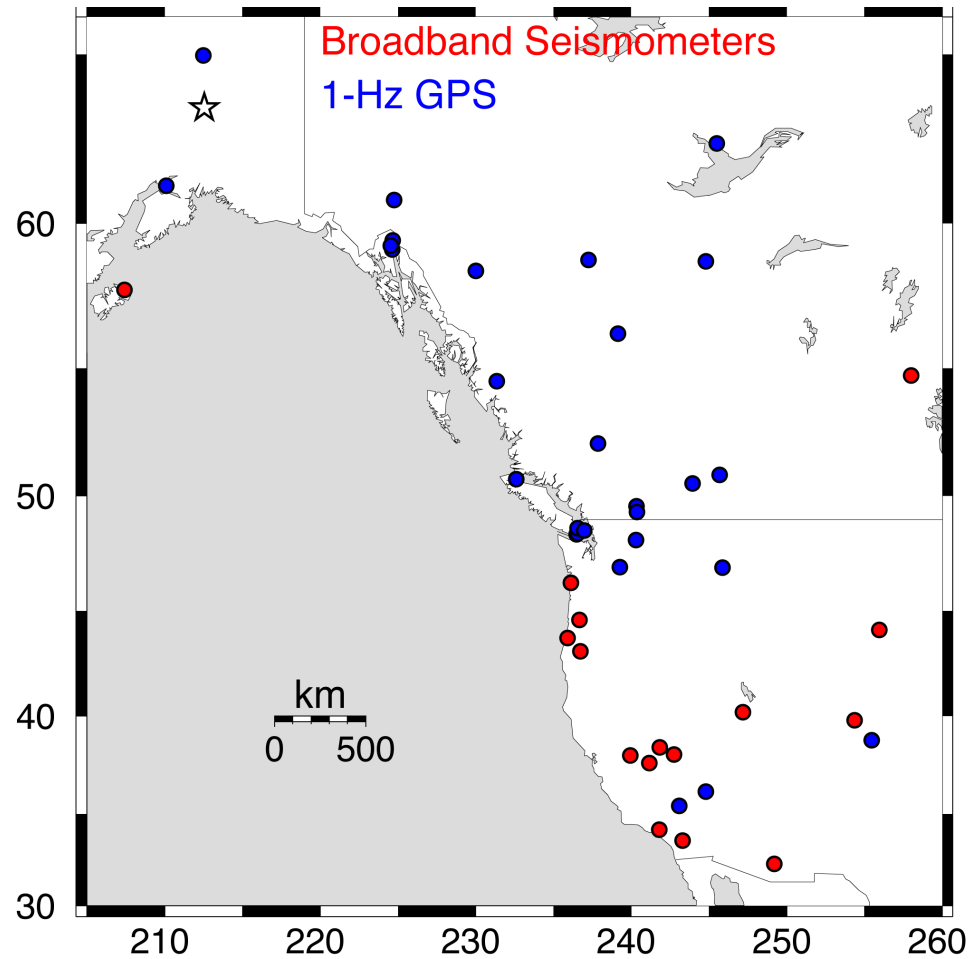


# Denali Seismic Instrumentation

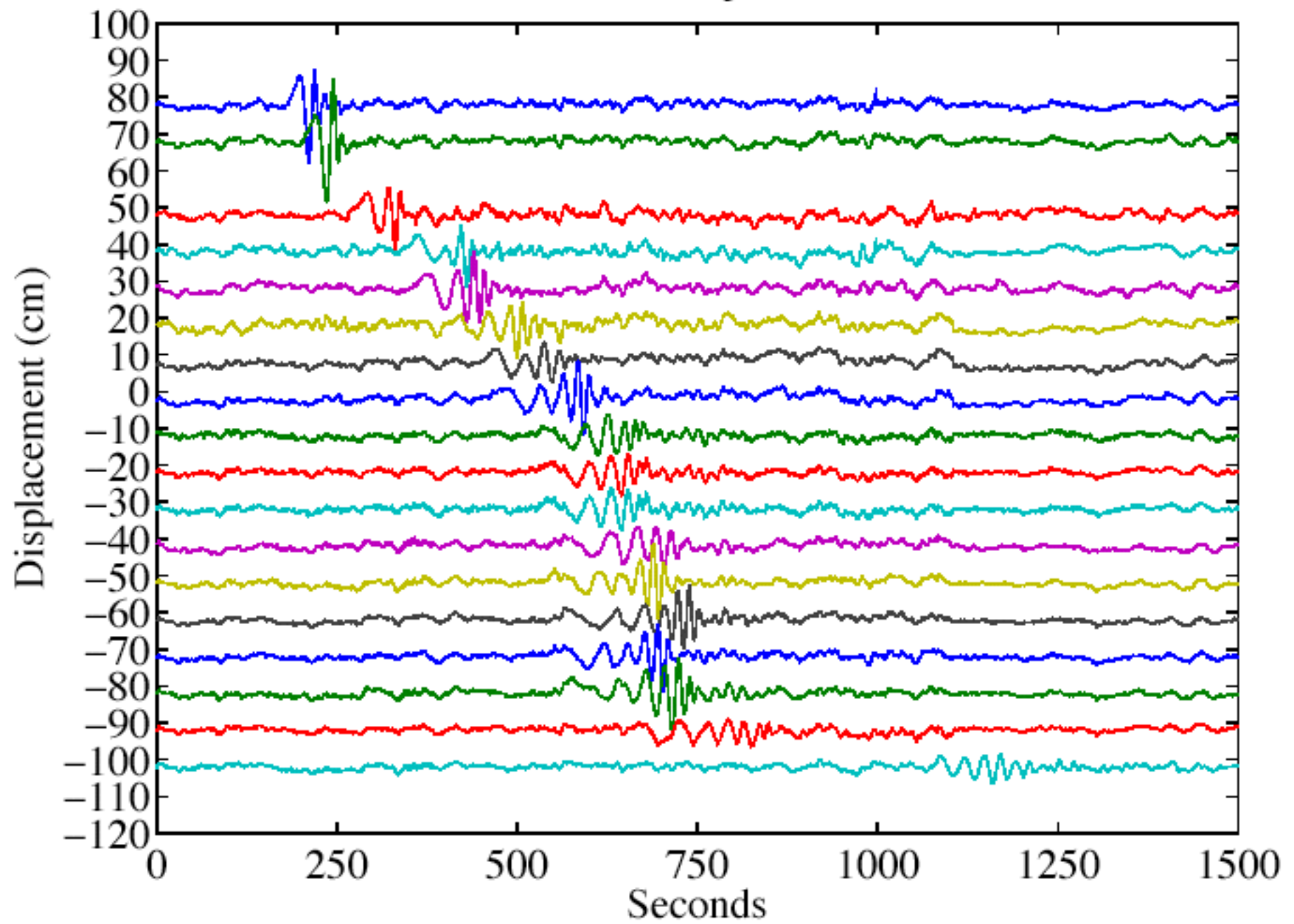


Sites that clipped (went off scale) removed

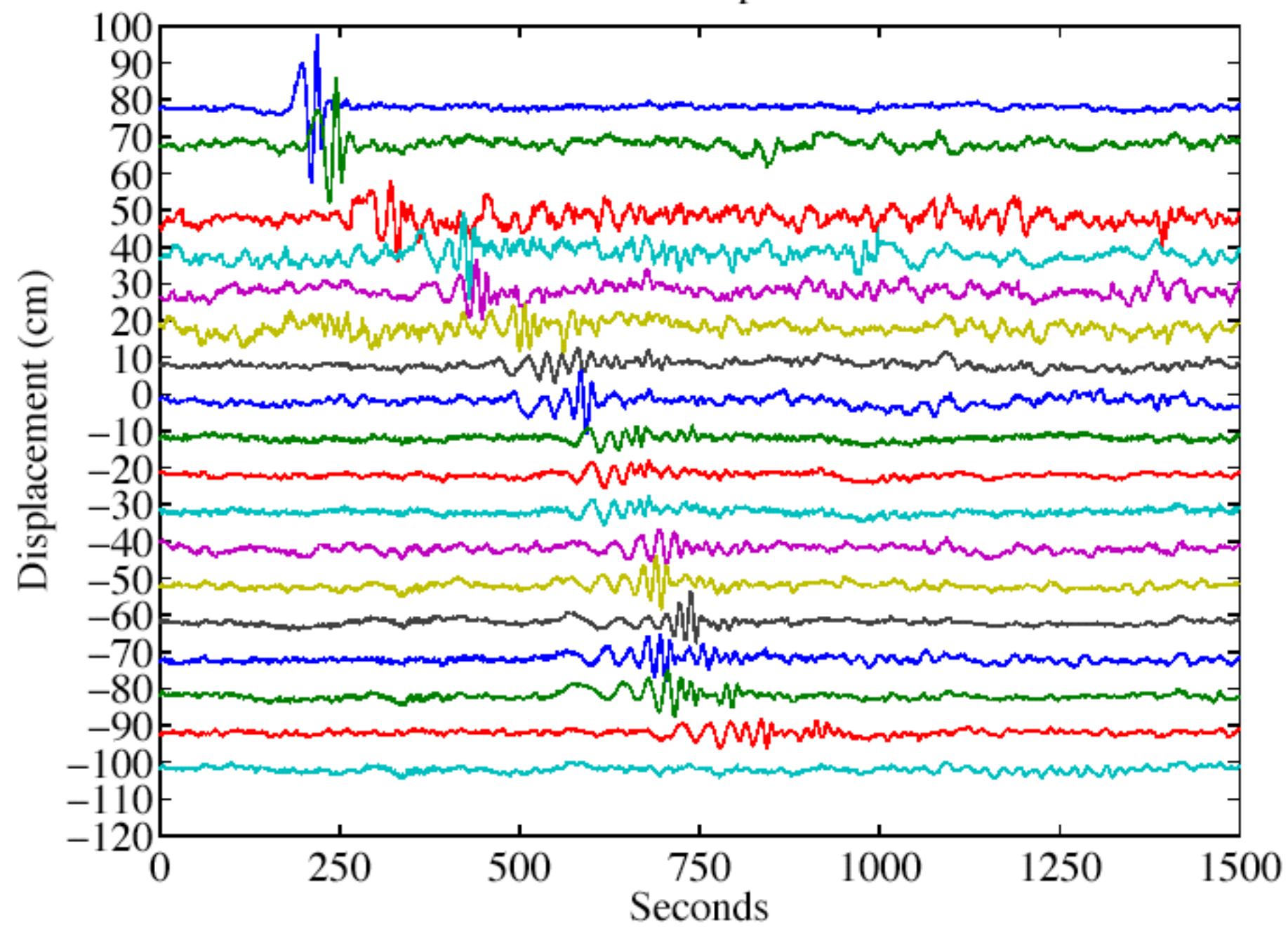
# Denali Seismic Instrumentation



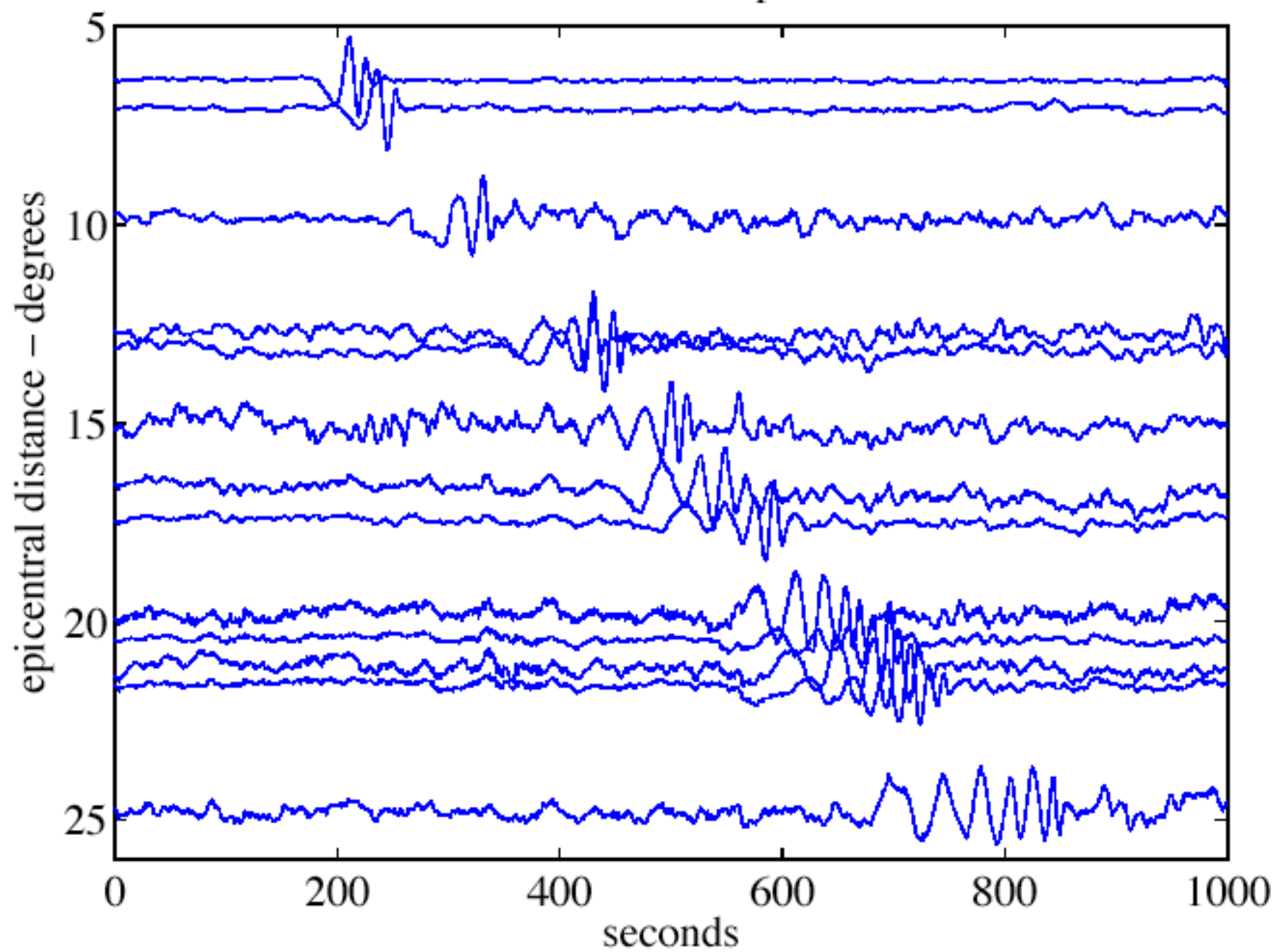
# East Component



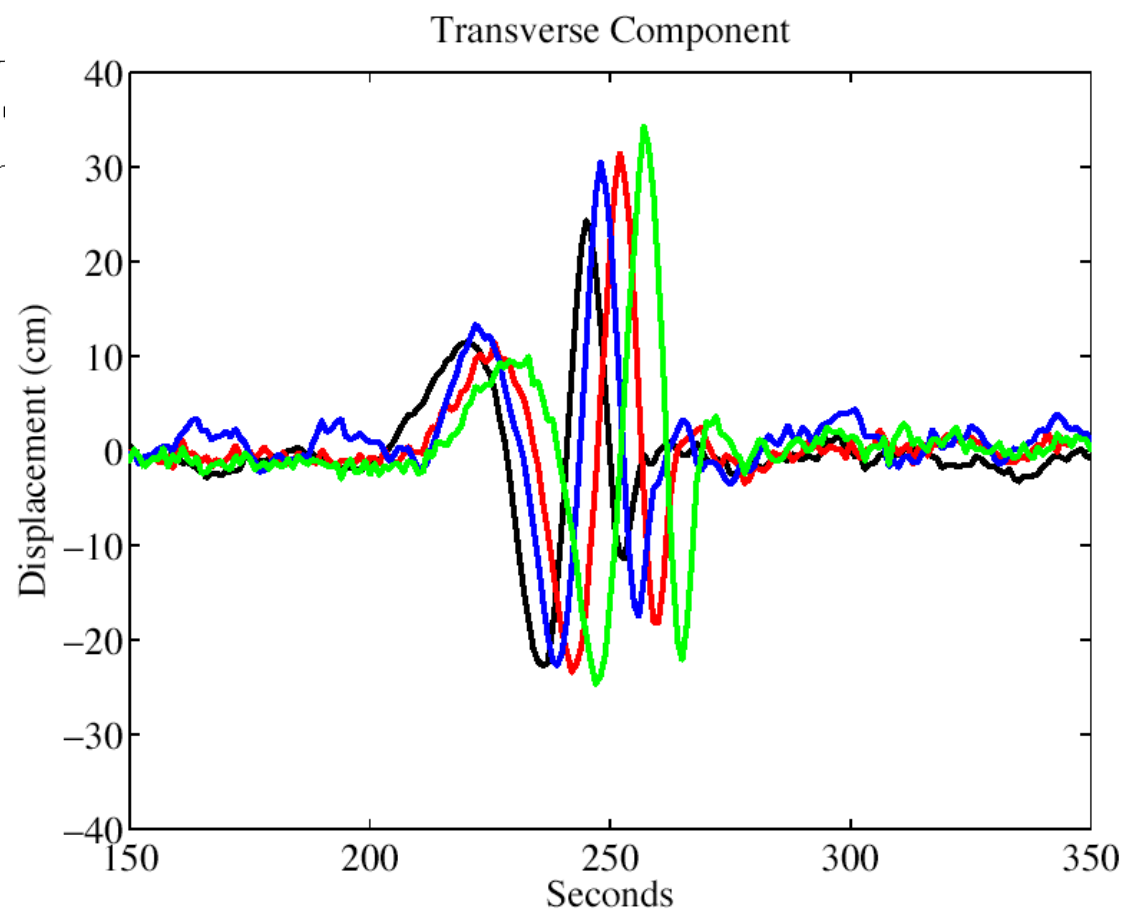
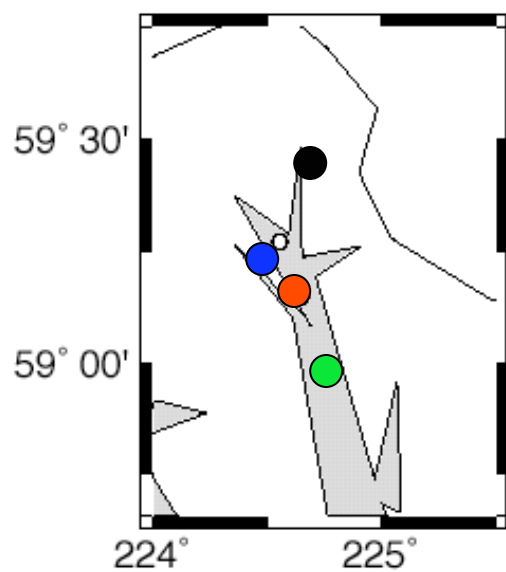
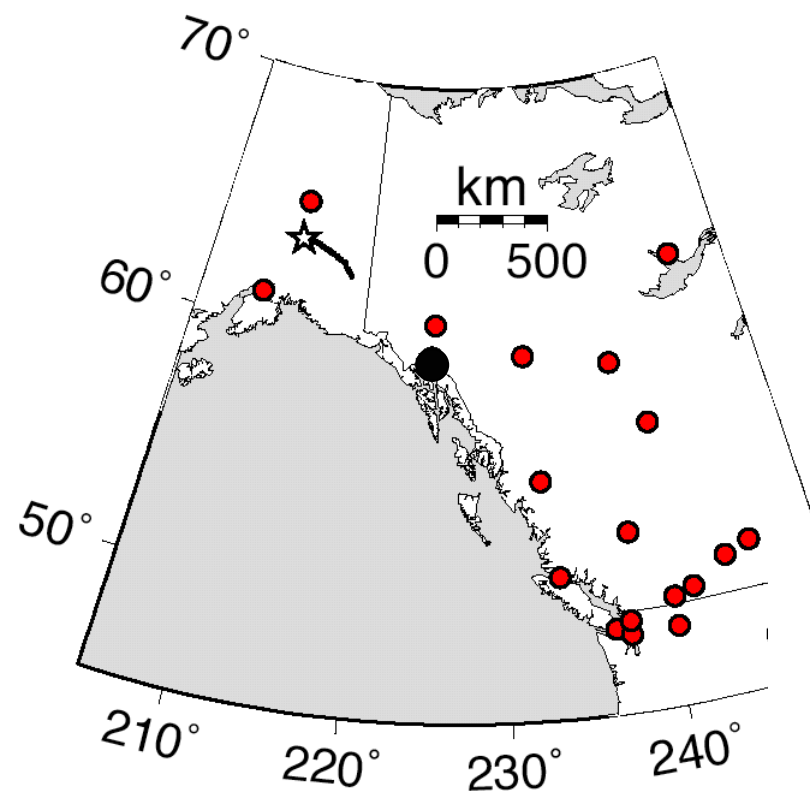
# North Component



# Transverse Component



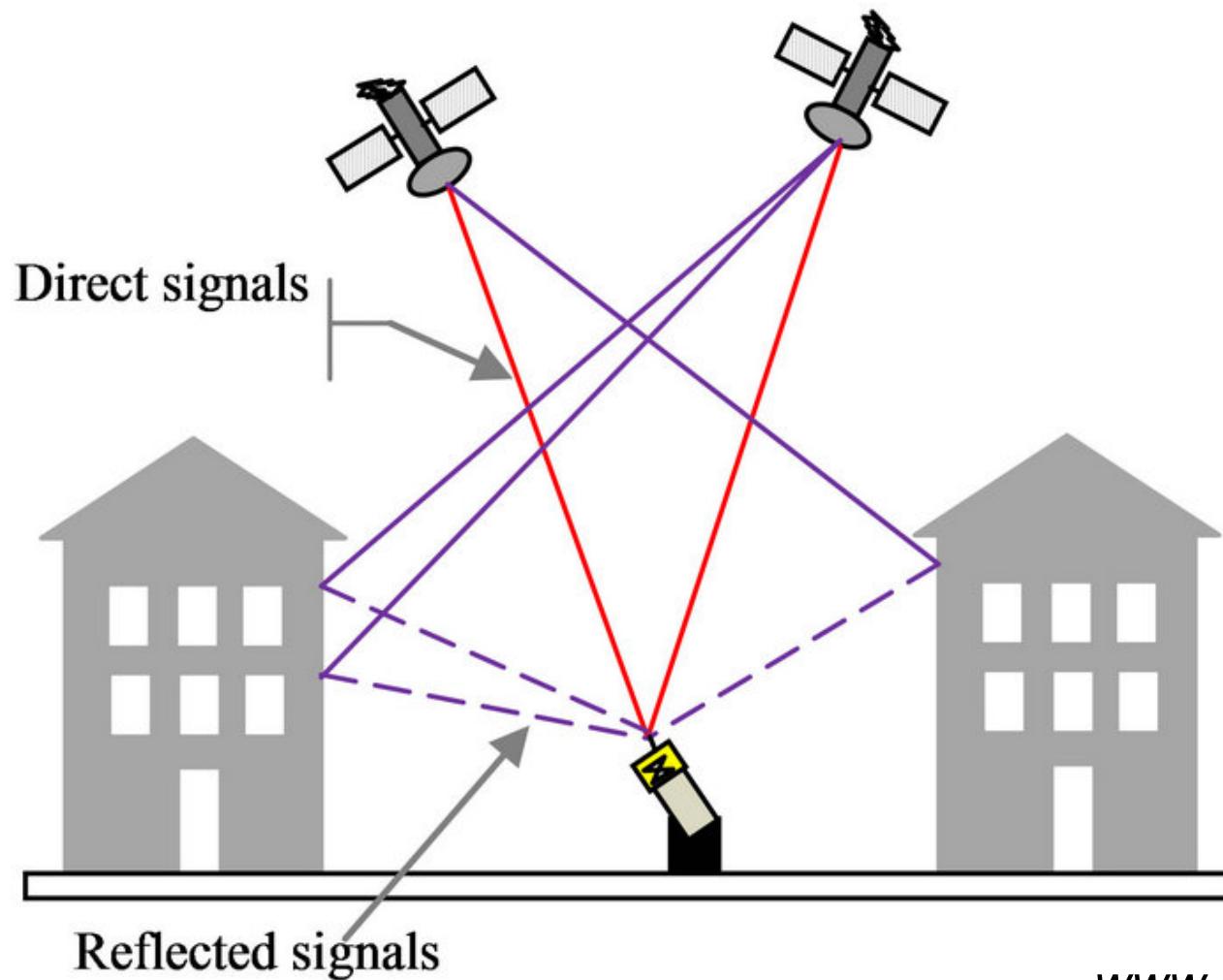




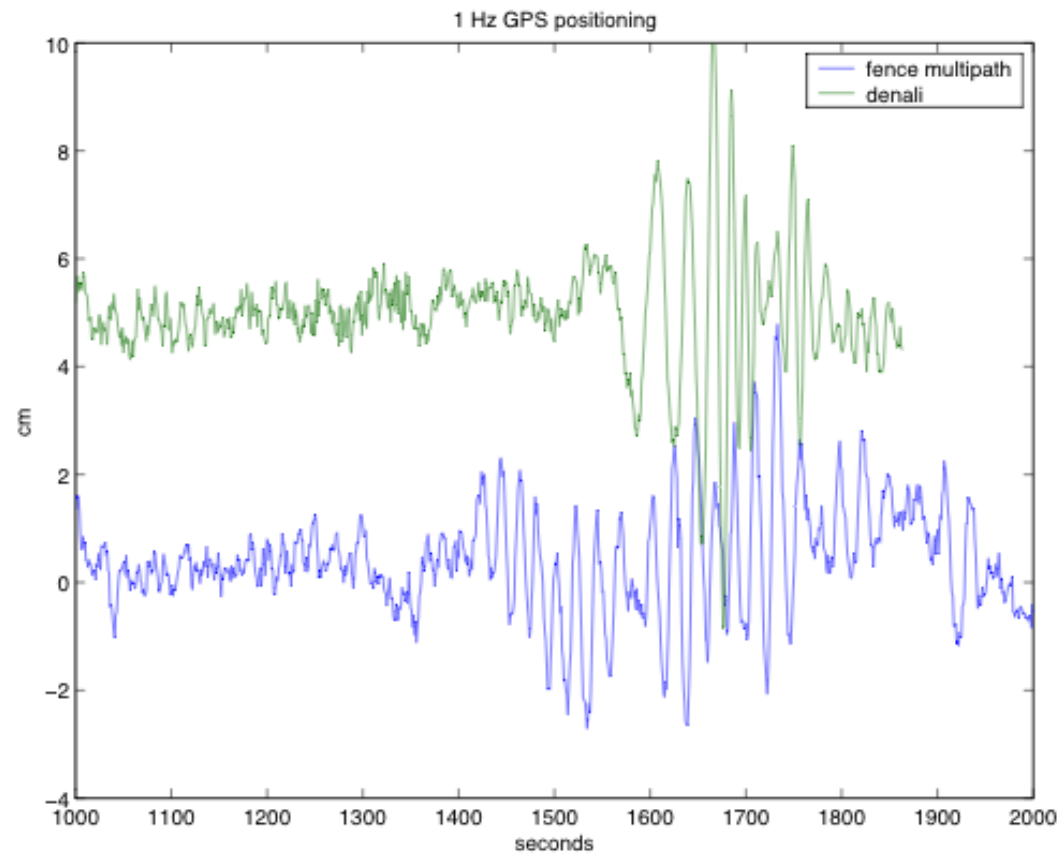
# Capabilities

- Precise enough to supplement traditional strong motion in earthquake source model inversions (Chen et al., 2004).
- No maximum displacement limit
  - But receivers may have tracking problems at extreme accelerations (e.g., 2010 Maule eq)
- No drift or tilt (off-level) errors
- But higher noise level than seismometers at high frequencies.

# Multipath



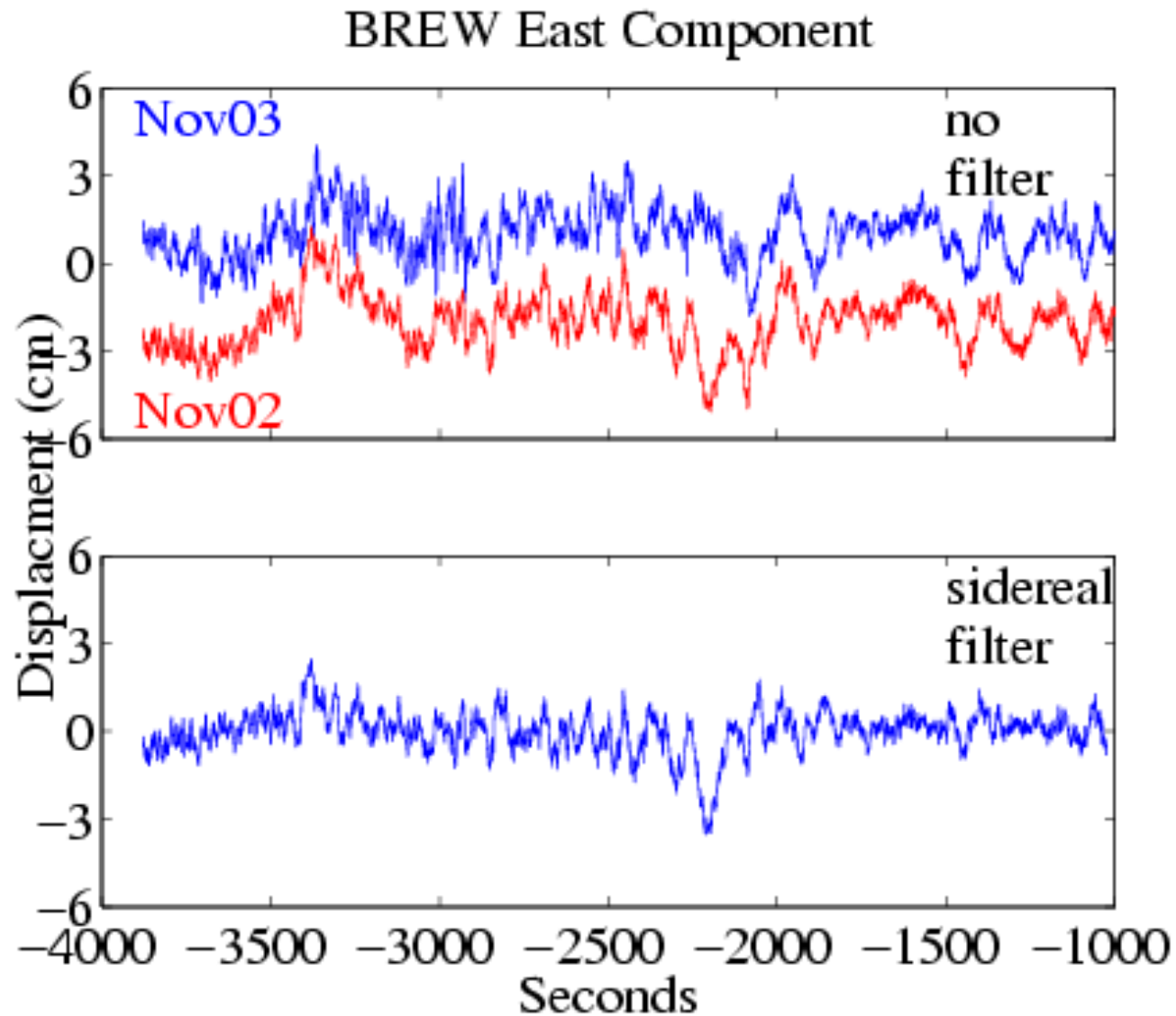
# Multipath



# Multipath and Sidereal Filtering

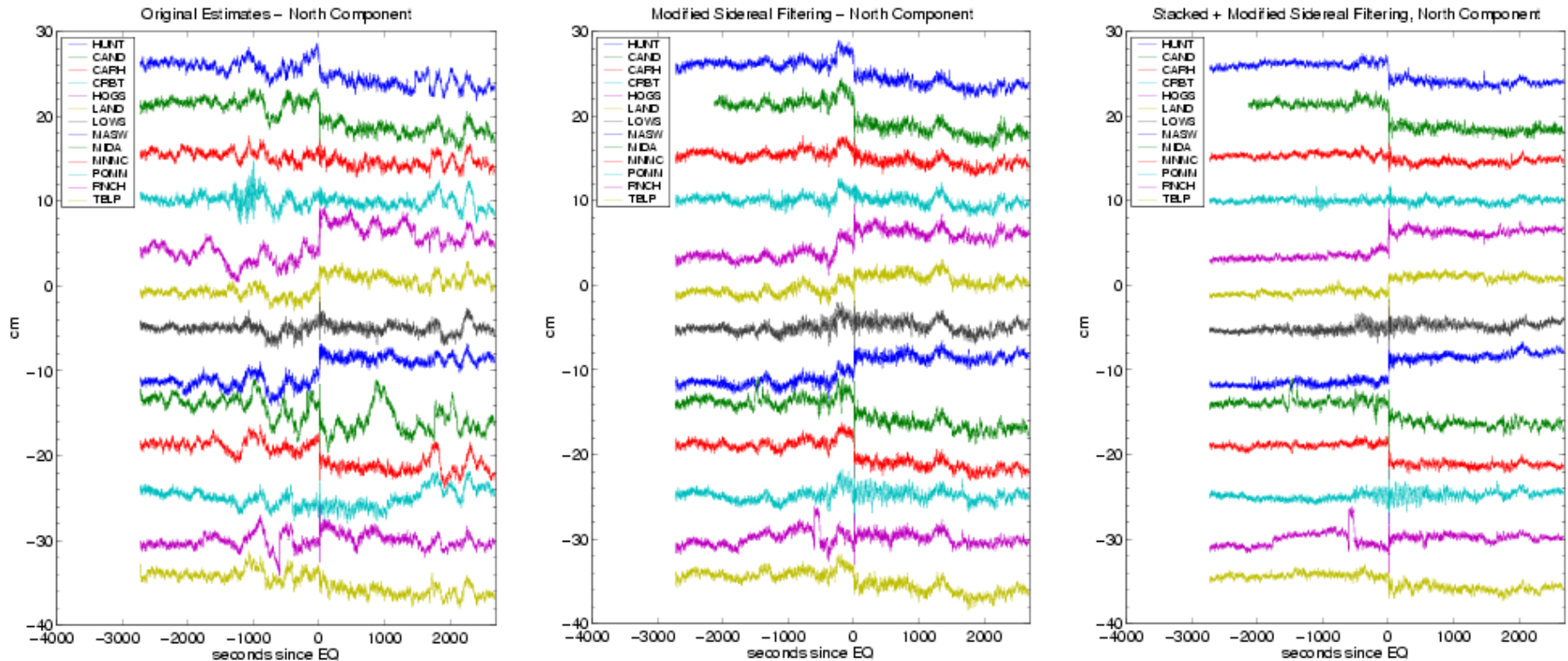
- The GPS orbital period  $\Rightarrow$  identical constellation geometry occurs 3 min 56 seconds earlier each day.
- Compute 1 Hz solutions for multiple days before and after the earthquake.
- Combine shifted solutions to remove “common” systematic errors.

## Example of sidereal shifting:



# Reducing Noise

## Parkfield earthquake



Andria Bilich, University of Colorado



# 2011 Tohoku-oki Earthquake



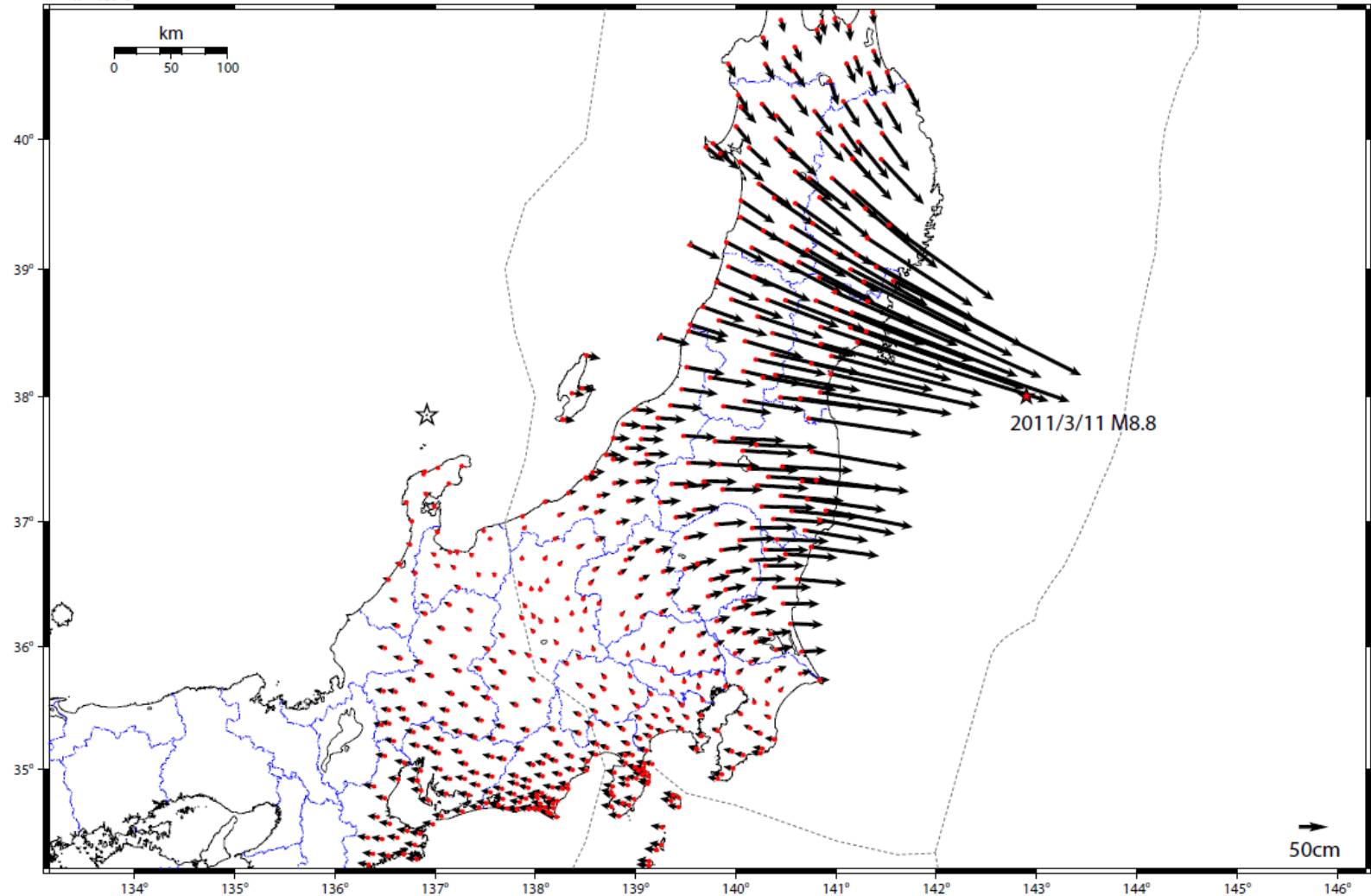


# Observed GPS Displacements

変動ベクトル図（水平）

基準期間：2011/03/01 21:00 - 2011/03/08 21:00  
比較期間：2011/03/11 16:30 - 2011/03/11 16:30

[http://www.jishin.go.jp/main/chousa/11mar\\_sanriku-oki/](http://www.jishin.go.jp/main/chousa/11mar_sanriku-oki/)



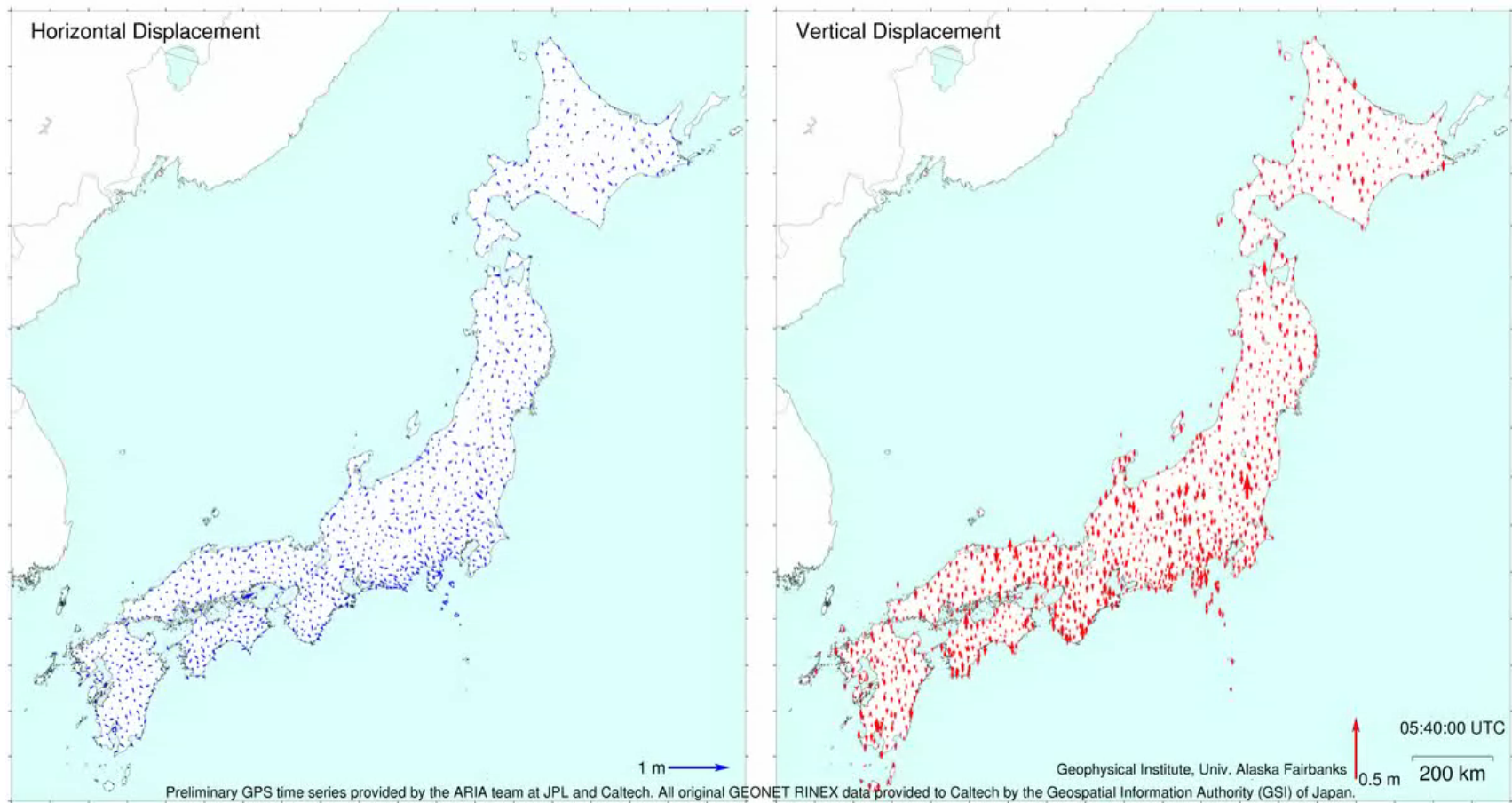
[基準：R3速報解 比較：S3迅速解]

☆固定局：舩倉島（950252）

国土地理院

Ronni Grapenthin  
*University of Alaska Fairbanks*

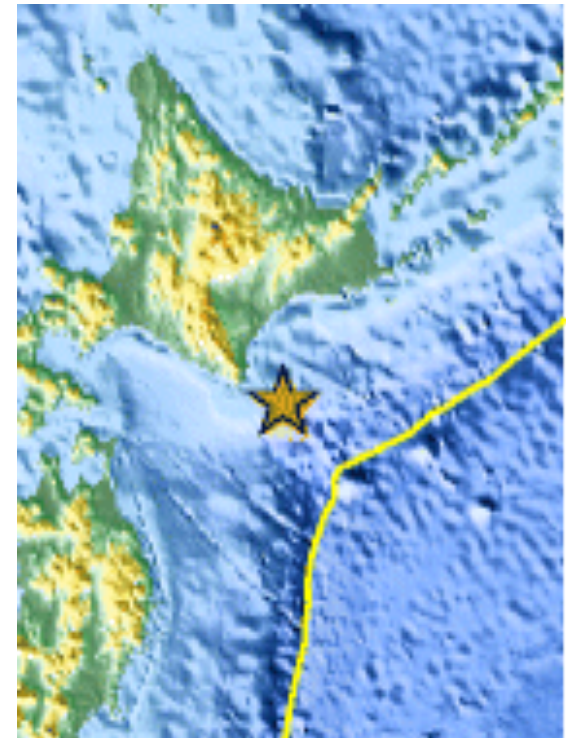
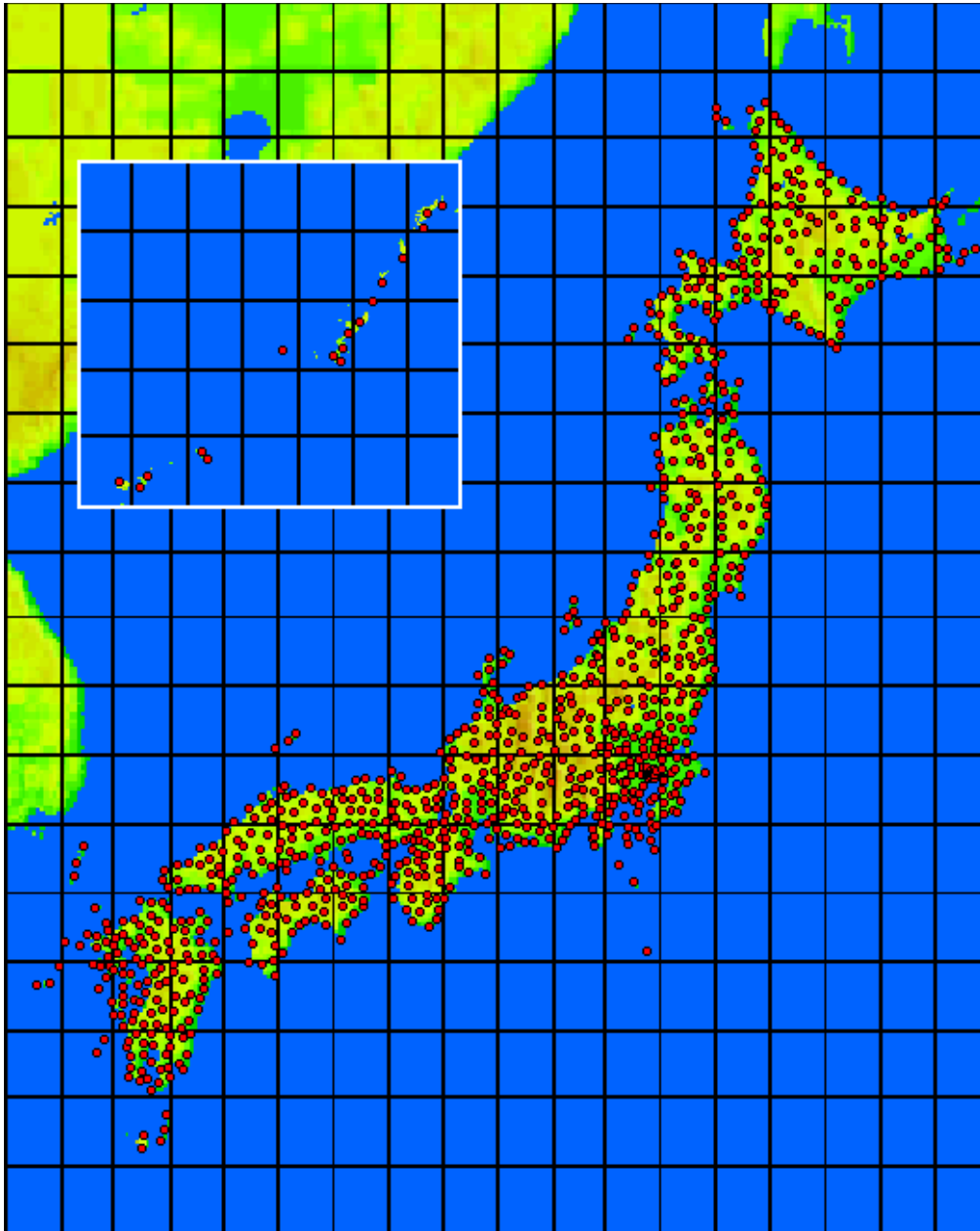
# Movie of an Earthquake



# 2003 September 25 Tokachi-Oki (Hokkaido) Earthquake



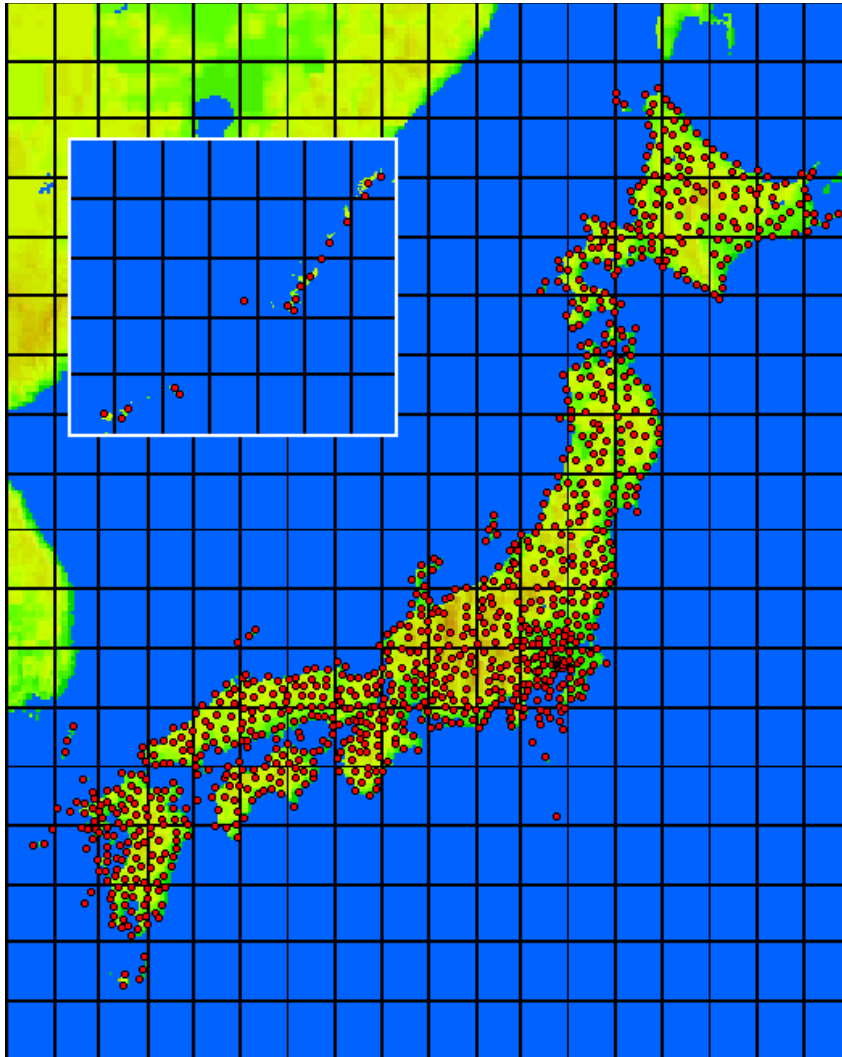
# Strong Motion Network



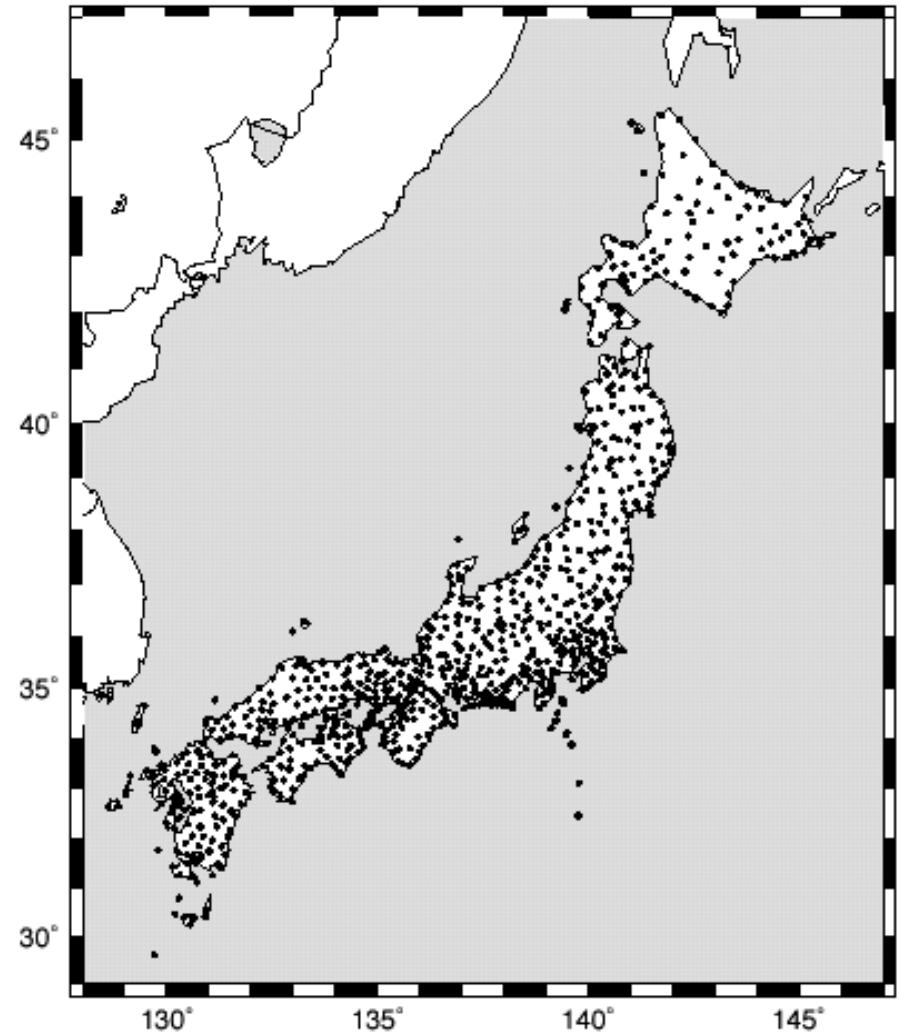
Harvard Mw 8.3



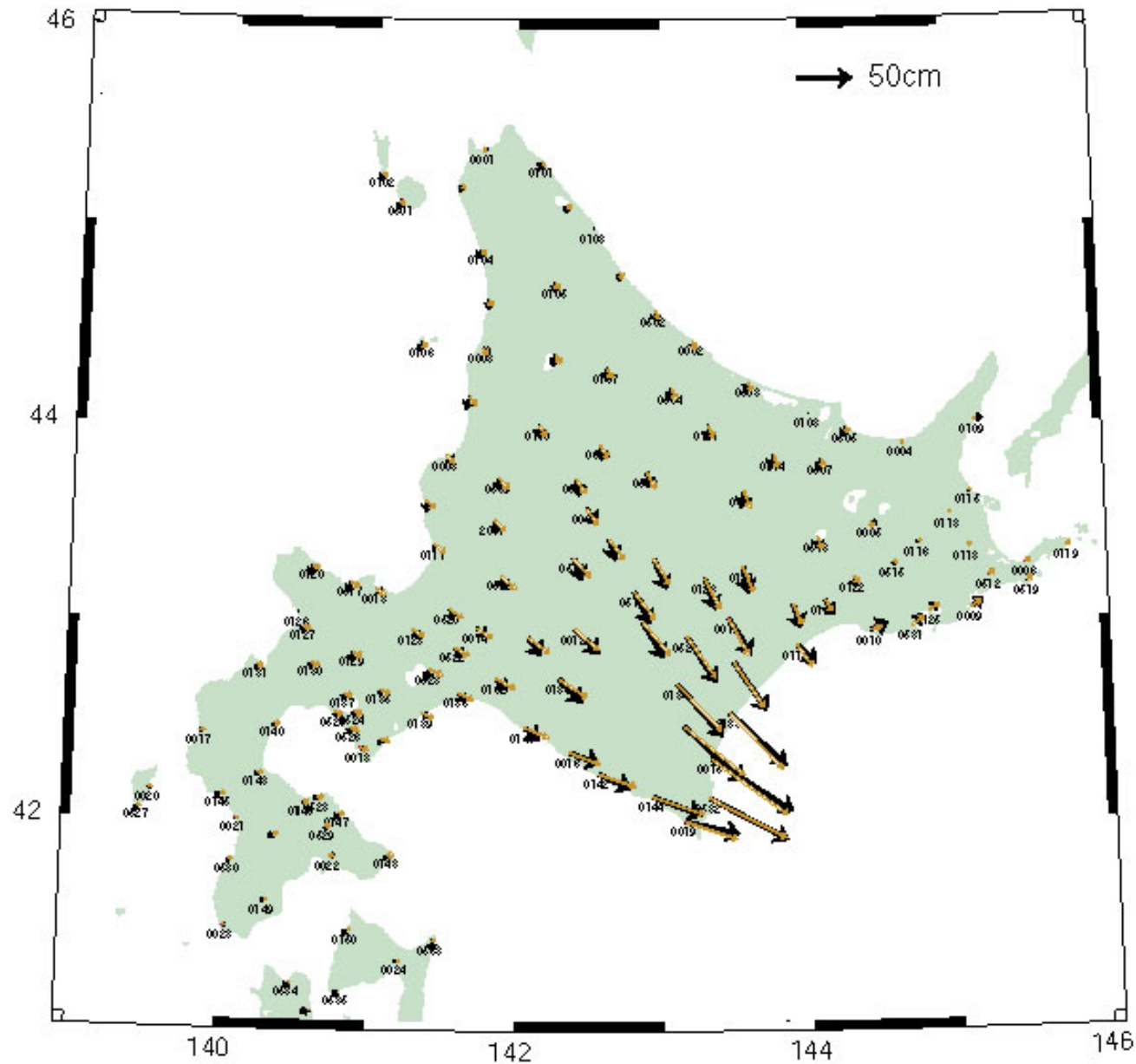
## Strong Motion Network



## GPS Network



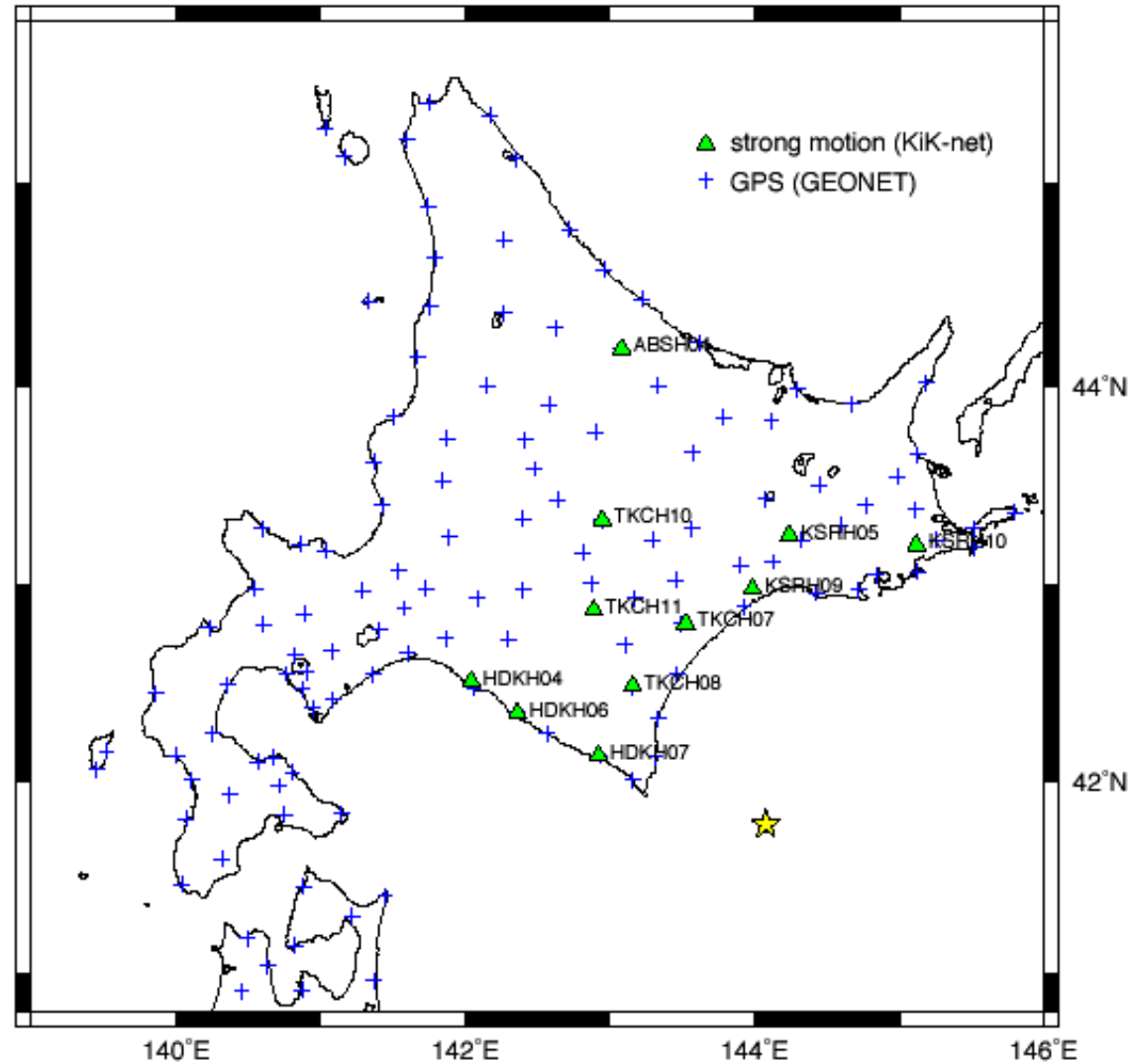
# Coseismic Displacements: traditional GPS



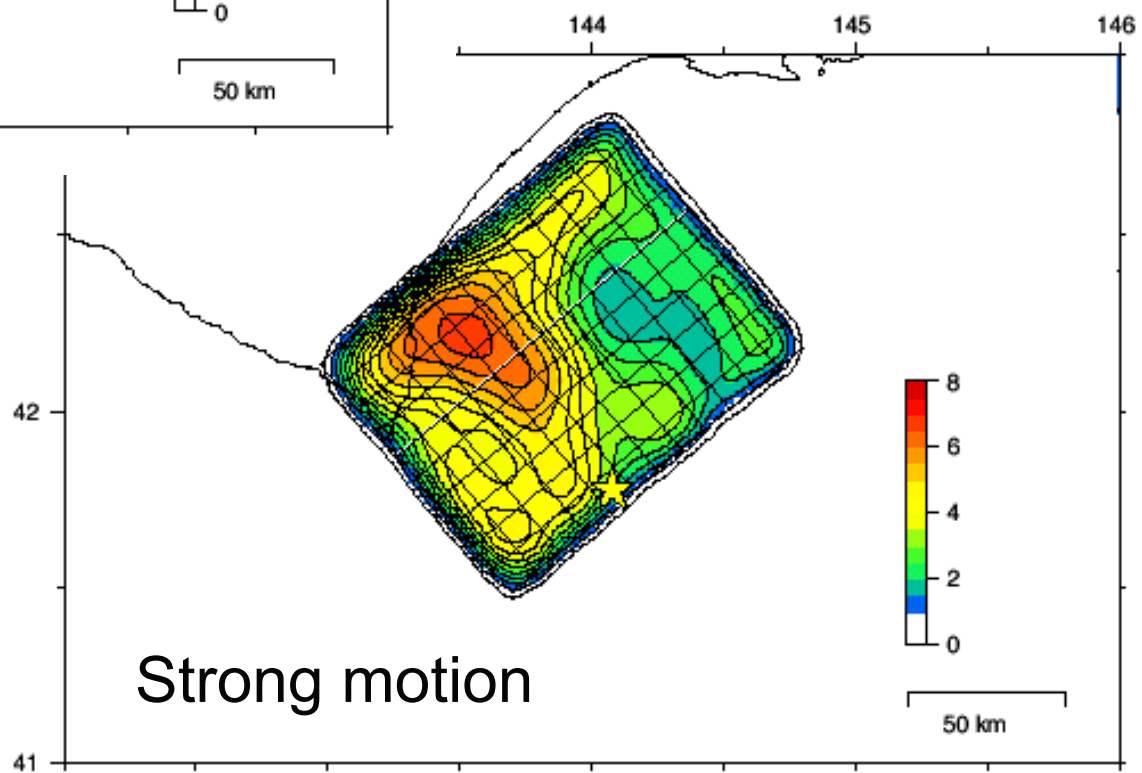
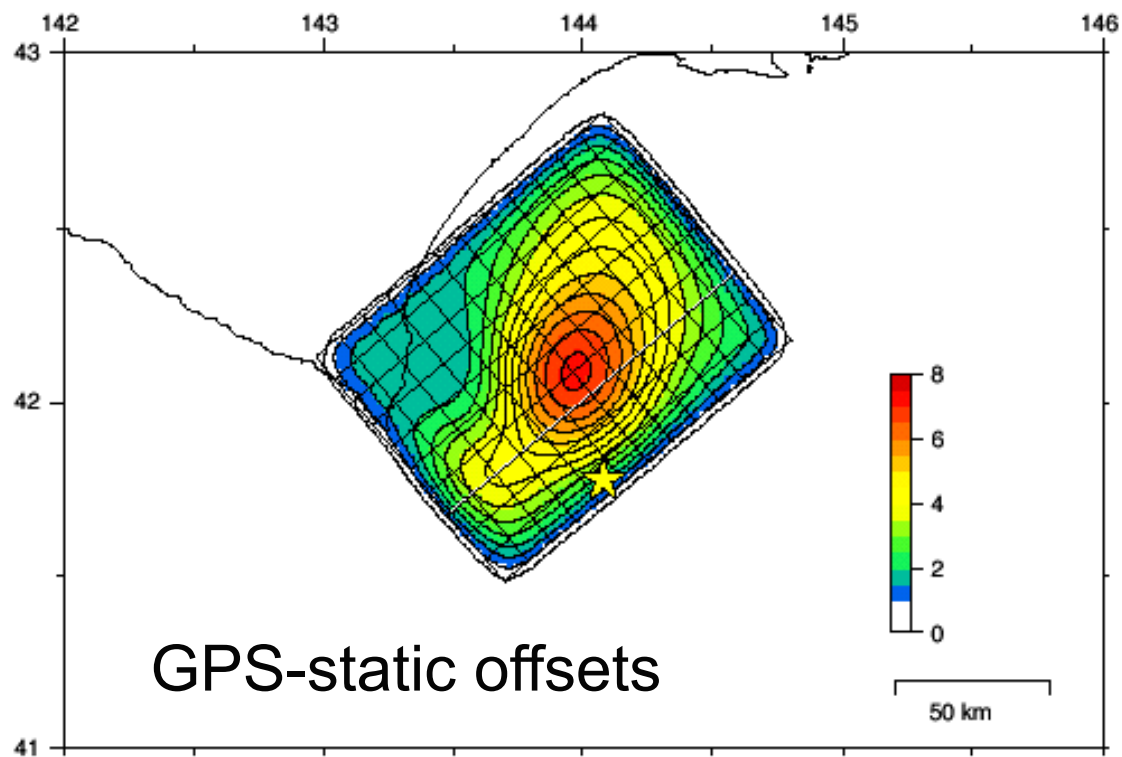
T. Kato  
Tokyo University

図2：地震時水平変動の観測値と計算値の比較

# Inversion for Rupture



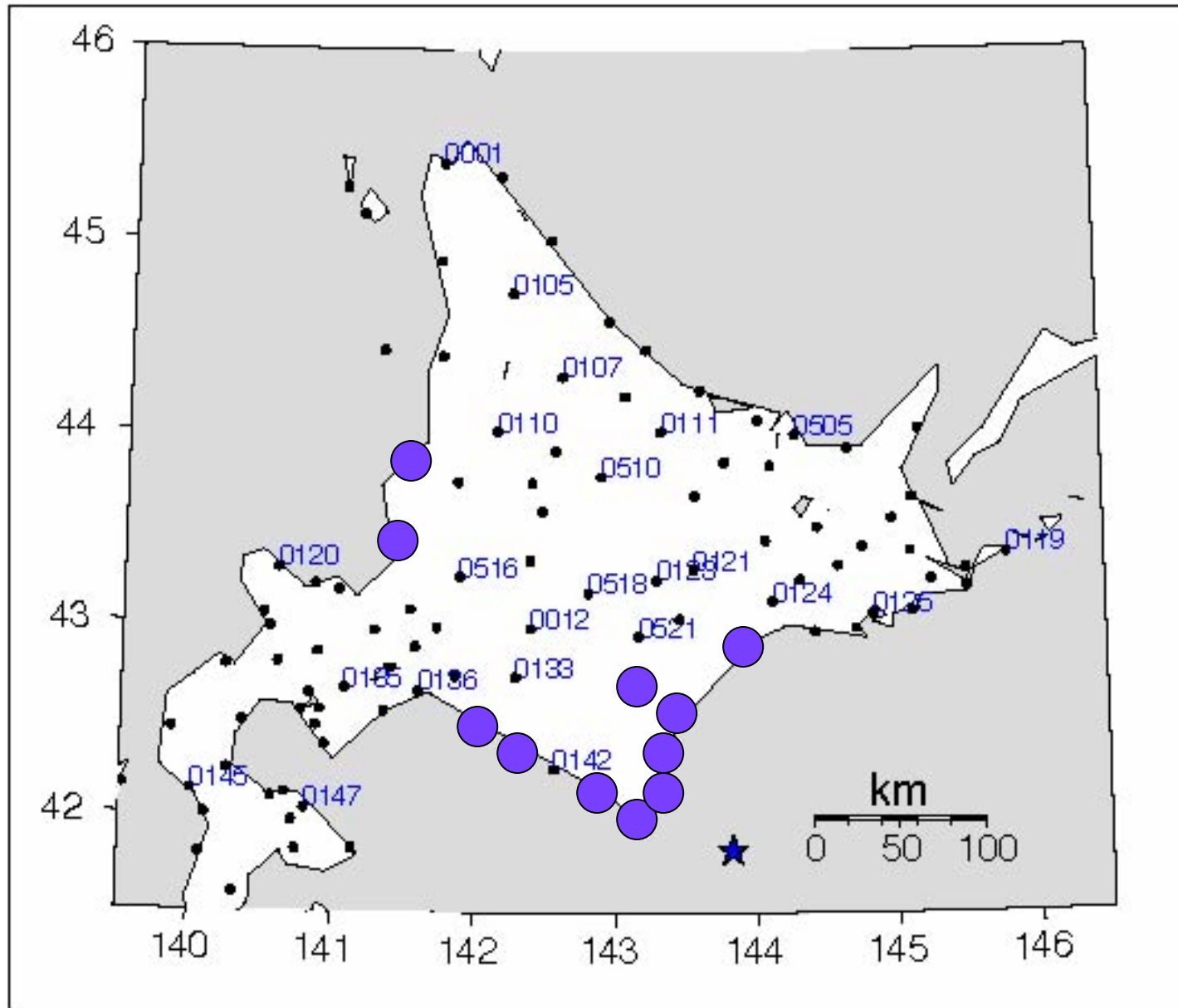
Koketsu et al.



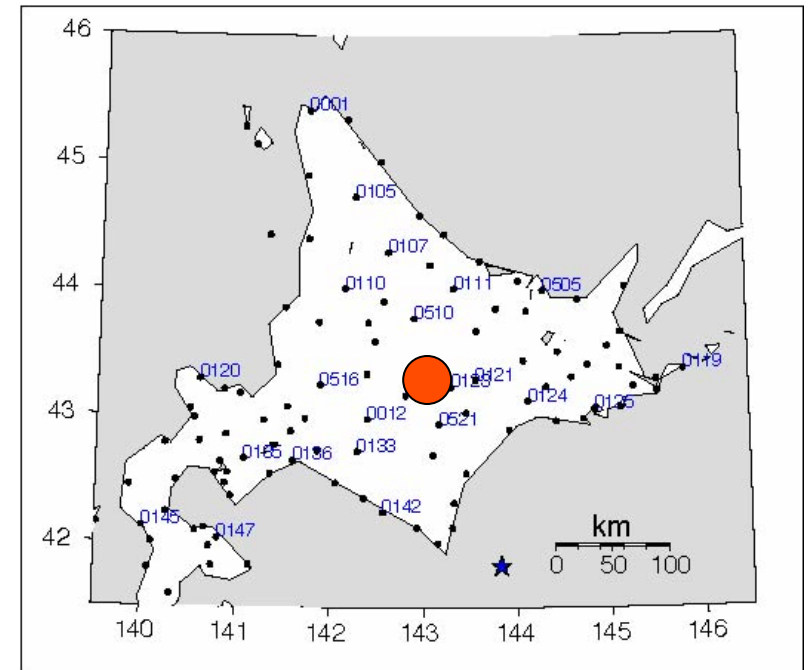


# 1-Hz GPS Sites

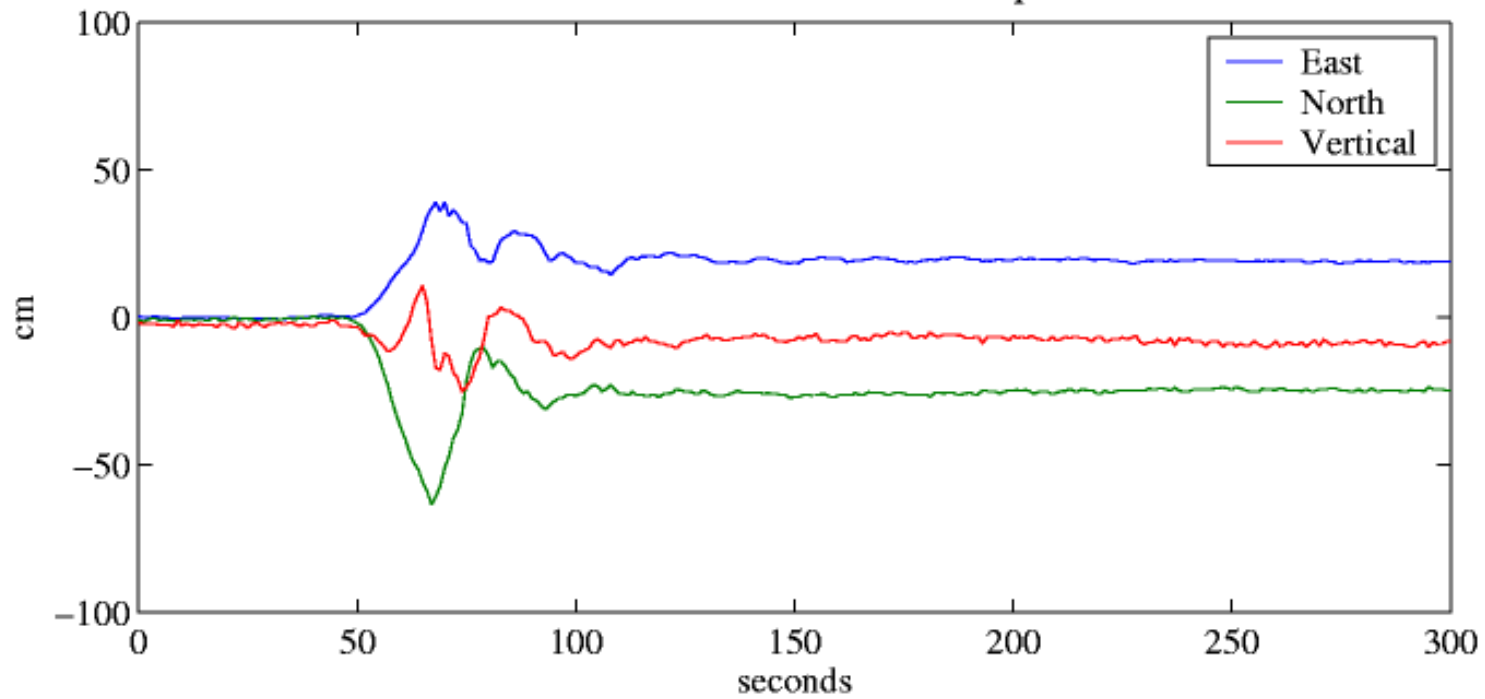
● Lost power



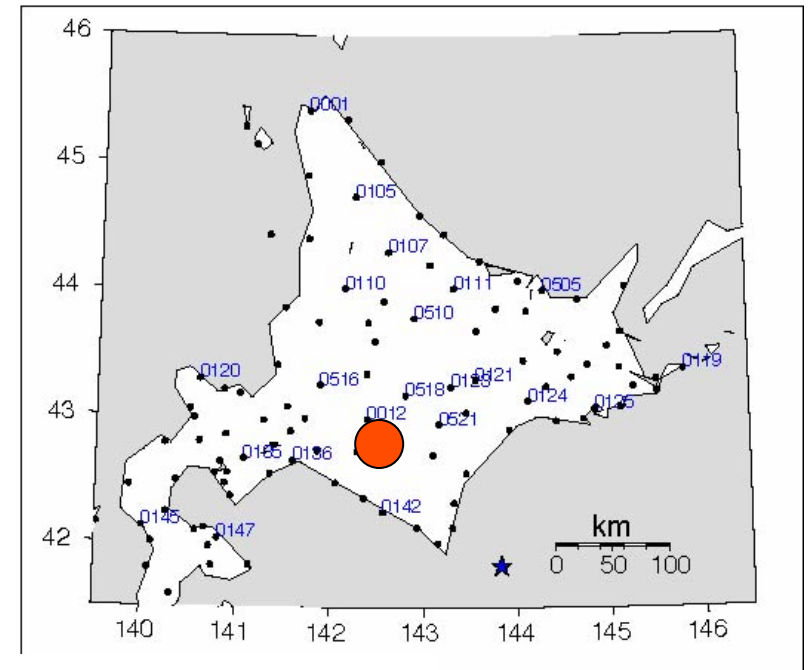
# 1 Hz GPS Position Estimates



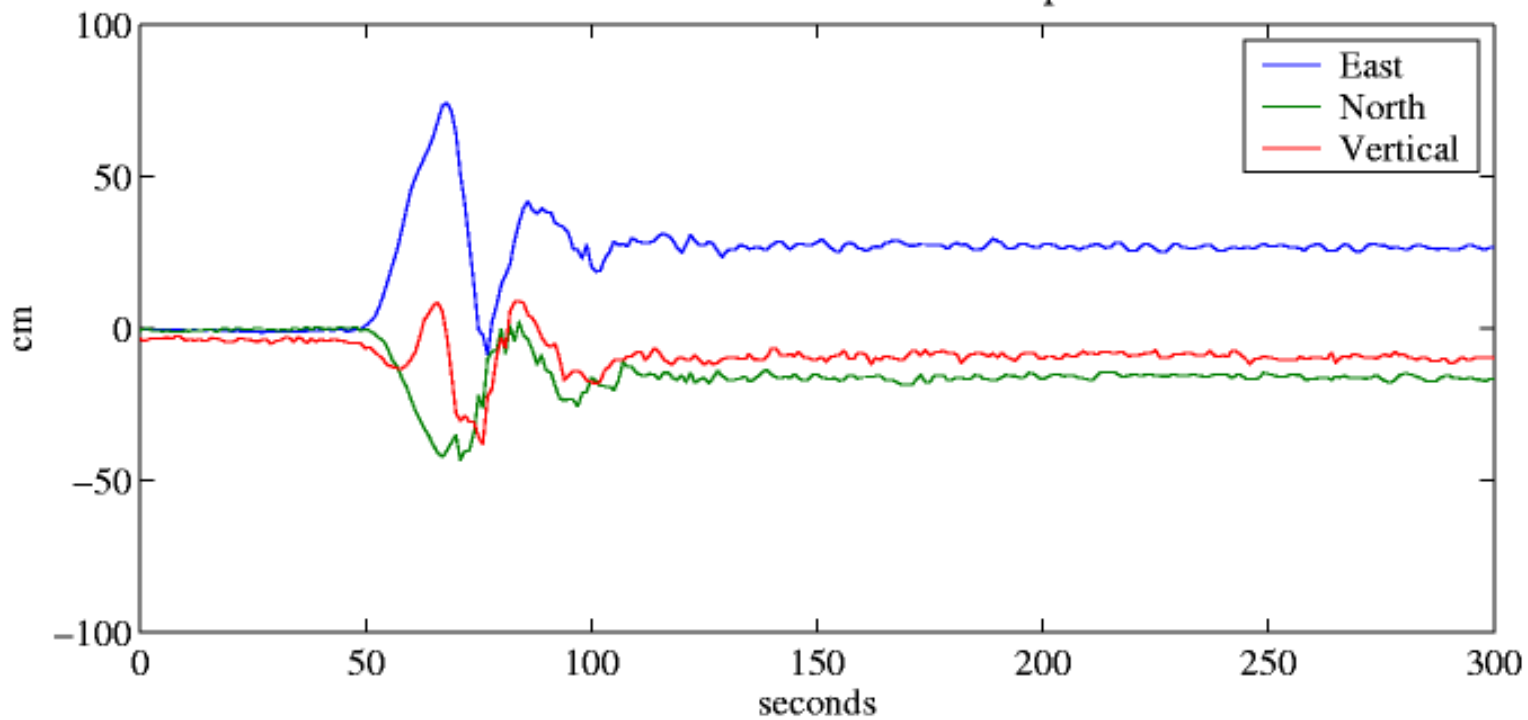
GPS Site 0518 Tokachi-Oki Earthquake



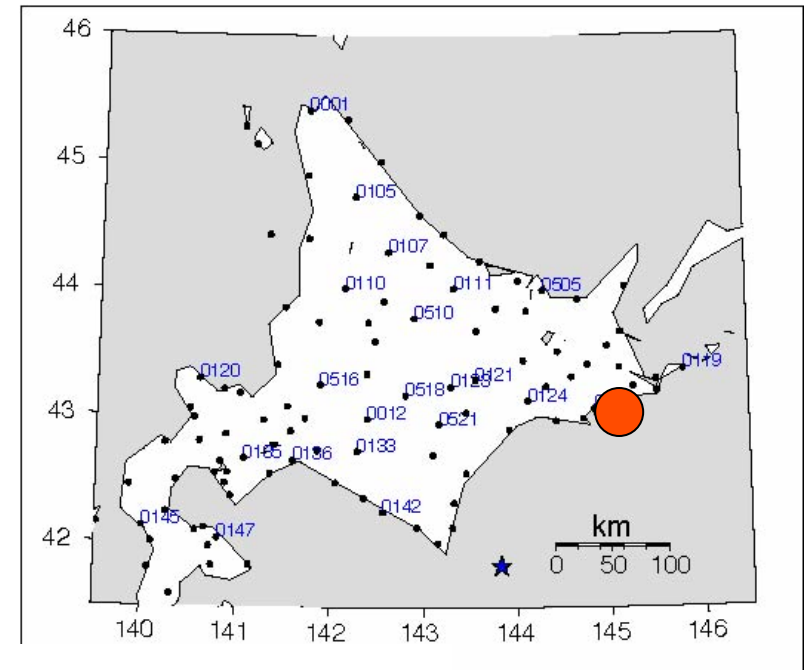
# 1 Hz GPS Position Estimates



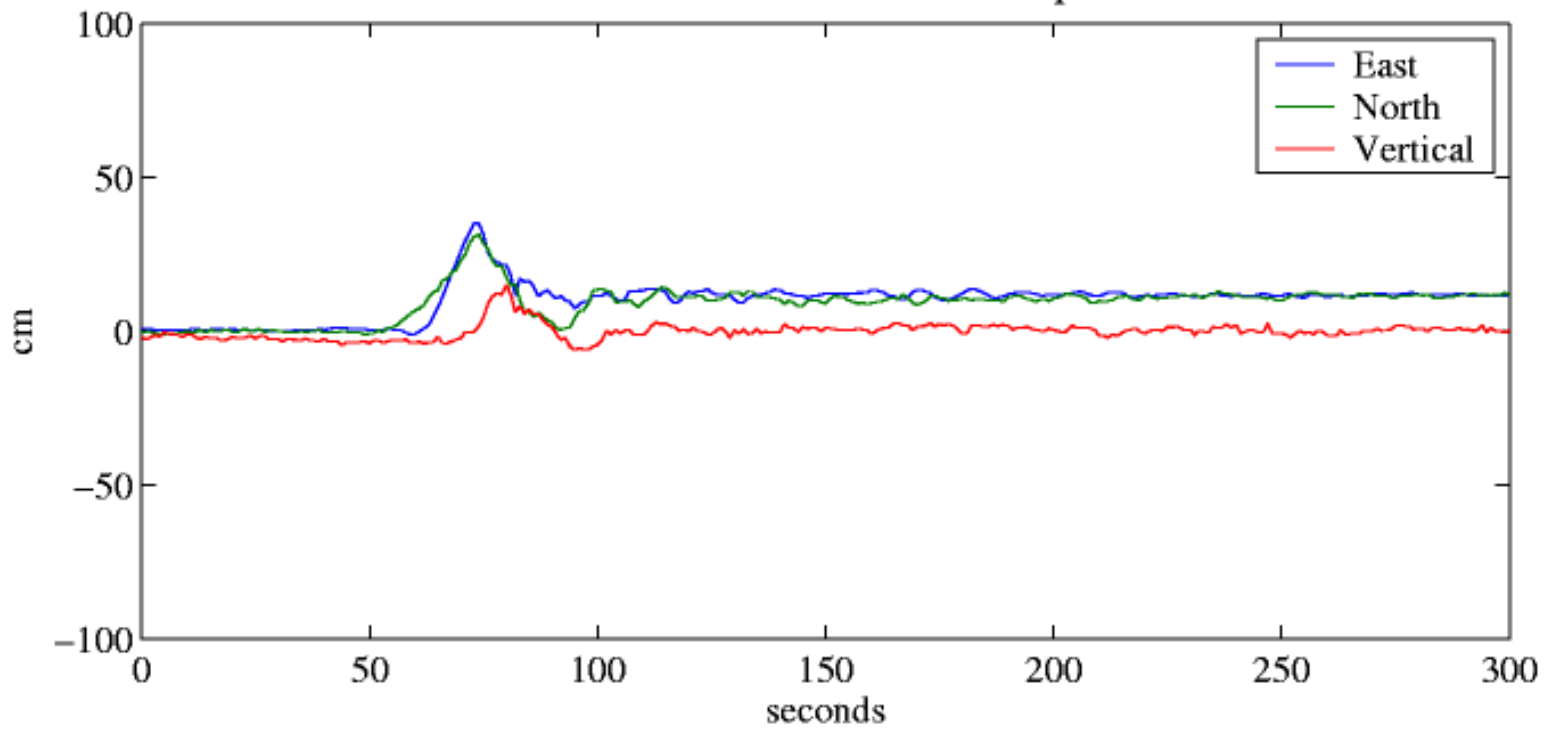
GPS Site 0133 Tokachi-Oki Earthquake

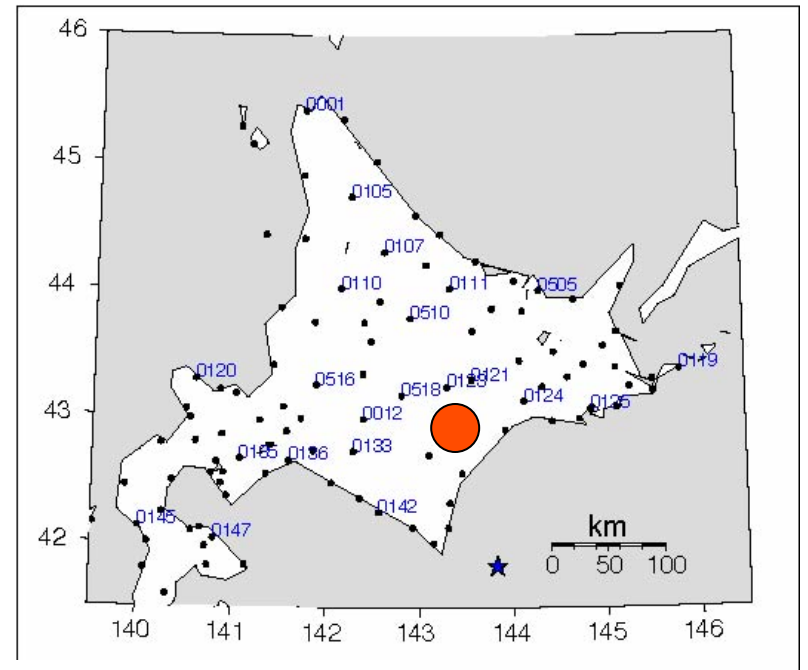


# 1 Hz GPS Position Estimates

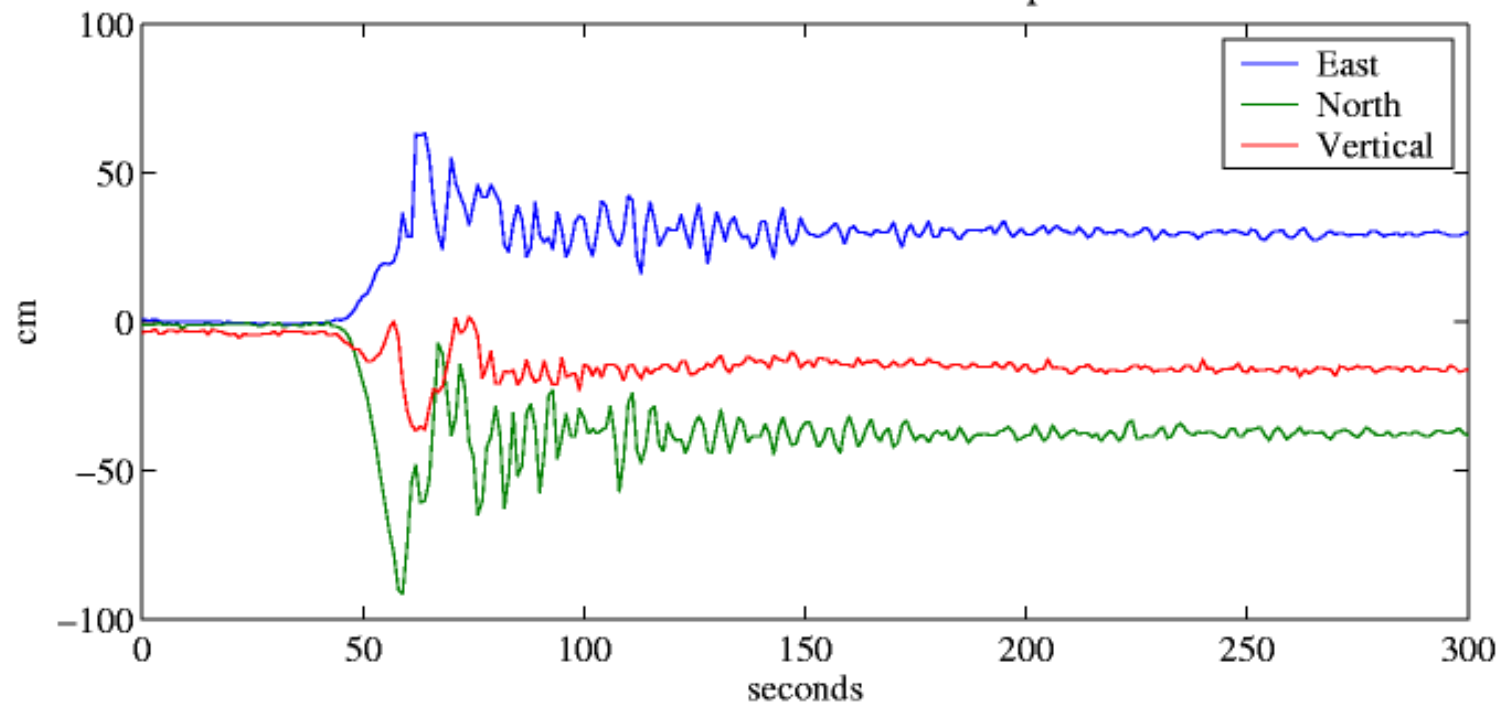


GPS Site 0125 Tokachi-Oki Earthquake

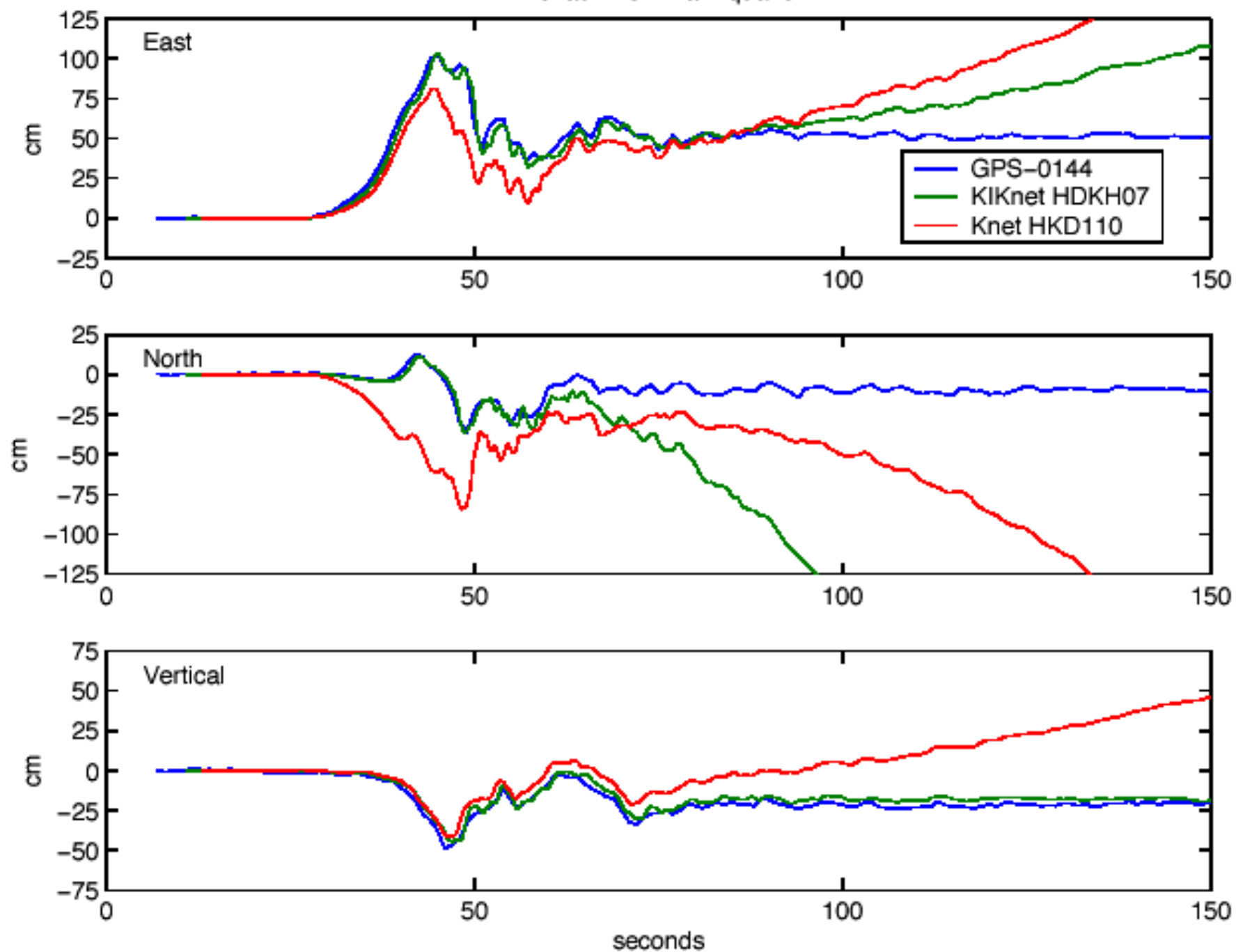




GPS Site 0521 Tokachi-Oki Earthquake

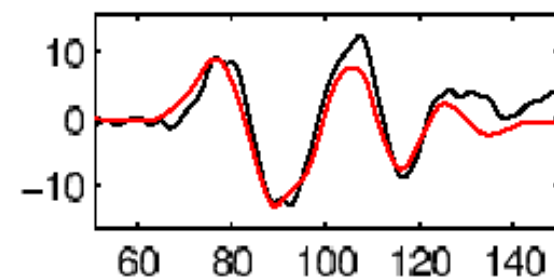
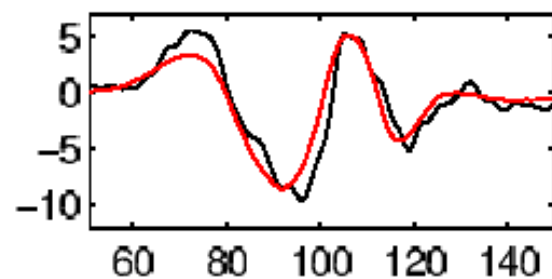
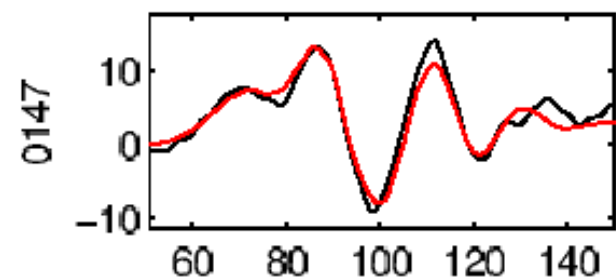
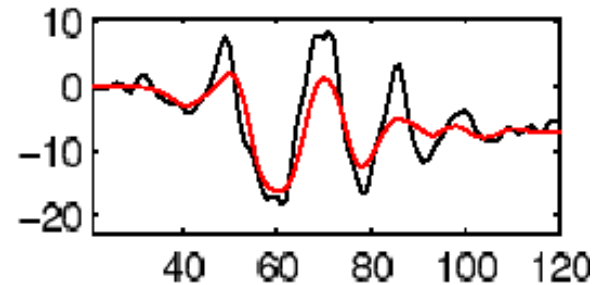
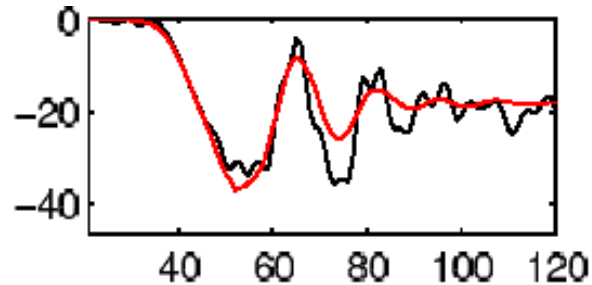
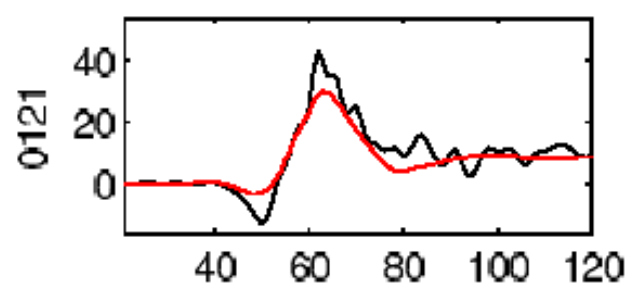
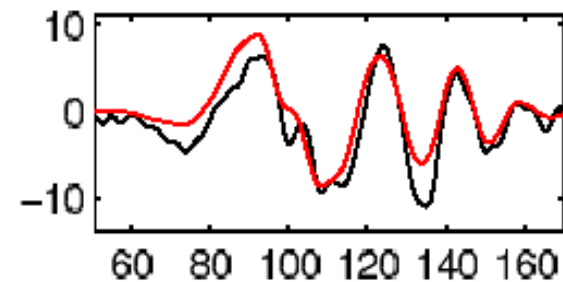
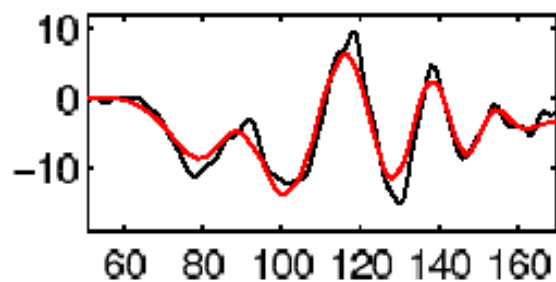
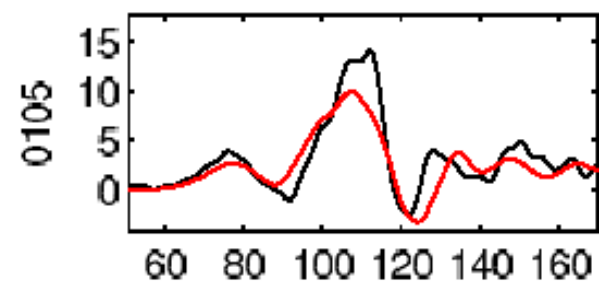
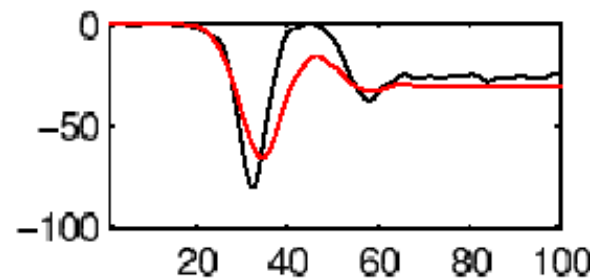
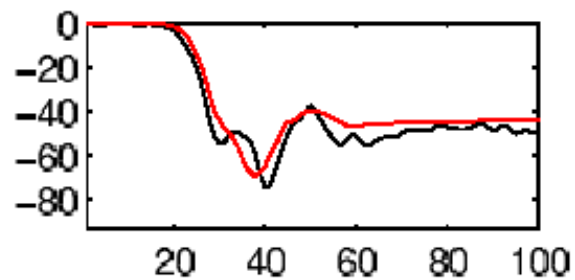
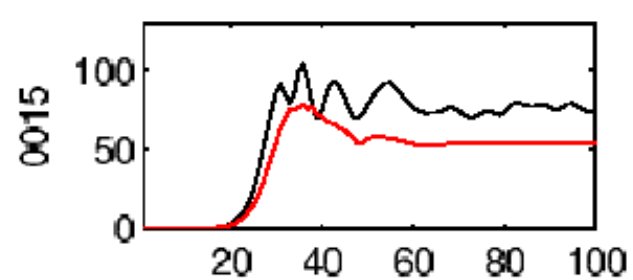


# Tokachi-Oki Earthquake



# Methodology

- Multiple time window inversion
- Fault plane 10 x 10 km segments
- Frequency-Wavenumber (FK) of *Zhu & Rivera* [2003].
- Smoothness & positivity constraints.
- Velocity structure after *Yagi* [2004].

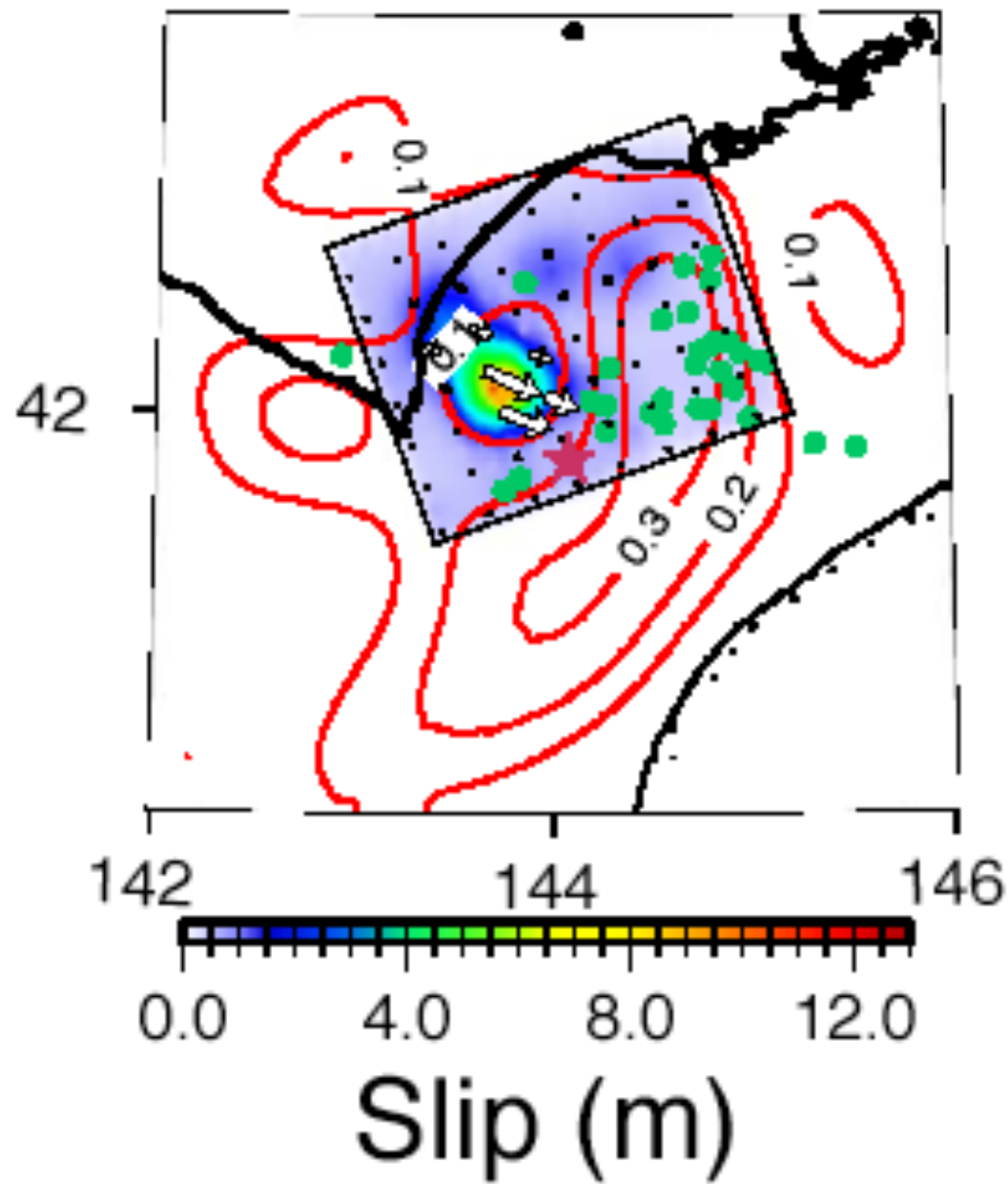


East

North

Vertical



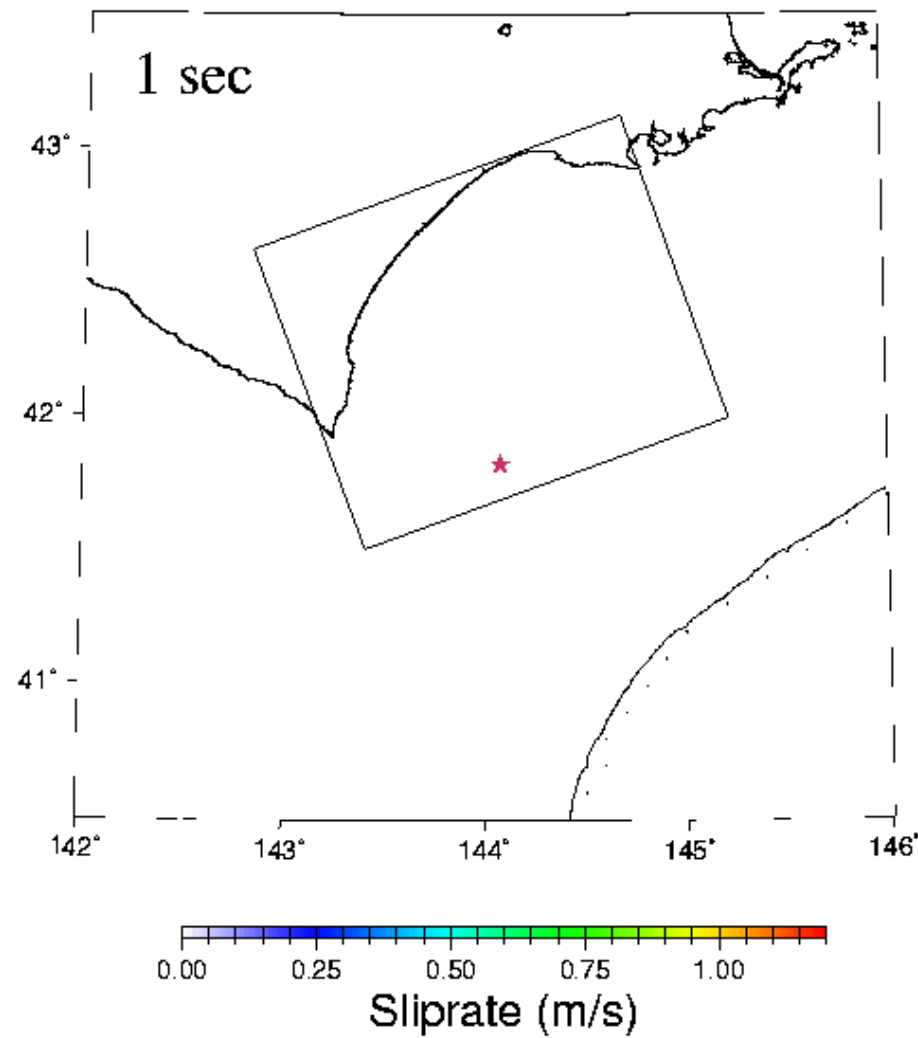


$M_0 = 1.7 \times 10^{21} \text{ Nm}$   
( $M_w 8.1$ )  
Peak Slip  $\sim 9.0 \text{ m}$

Aftershocks

*Ito et al.* [2004]

# Animated Slip Model



Miyazaki et al., 2004